

Compositional Shape Analysis by means of Bi-Abduction

Dino Distefano

Queen Mary University of London

and

Monoidics Ltd

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A lot of real code out there uses pointer manipulation...

```
void t1394Diag_CancelIrp(PDEVICE_OBJECT DeviceObject, PIRP Irp)
{
    KIRQL           Irql, CancelIrql;
    BUS_RESET_IRP   *BusResetIrp, *temp;
    PDEVICE_EXTENSION deviceExtension;

    deviceExtension = DeviceObject->DeviceExtension;

    KeAcquireSpinLock(&deviceExtension->ResetSpinLock, &Irql);

    temp = (PBUS_RESET_IRP)deviceExtension;
    BusResetIrp = (PBUS_RESET_IRP)deviceExtension->Flink2;

    while (BusResetIrp) {

        if (BusResetIrp->Irp == Irp) {
            temp->Flink2 = BusResetIrp->Flink2;
            free(BusResetIrp);
            break;
        }
        else if (BusResetIrp->Flink2 == (PBUS_RESET_IRP)deviceExtension) {
            break;
        }
        else {
            temp = BusResetIrp;
            BusResetIrp = (PBUS_RESET_IRP)BusResetIrp->Flink2;
        }
    }

    KeReleaseSpinLock(&deviceExtension->ResetSpinLock, Irql);

    IoReleaseCancelSpinLock(Irp->CancelIrql);
    Irp->IoStatus.Status = STATUS_CANCELLED;
    IoCompleteRequest(Irp, IO_NO_INCREMENT);
} // t1394Diag_CancelIrp
```

Is this correct?

Or at least: does it basic properties like it won't crash or leak memory?

We want to build tool that automatically answer such questions

Crash course on Separation Logic

Simple Imperative Language

- ⦿ Safe commands:

- ⦿ $S ::= \text{skip} \mid x := E \mid x := \text{new}(E_1, \dots, E_n)$

- ⦿ Heap accessing commands:

- ⦿ $A(E) ::= \text{dispose}(E) \mid x := [E] \mid [E] := F$

where E is and expression x, y, nil , etc.

- ⦿ Command:

- ⦿ $C ::= S \mid A \mid C_1; C_2 \mid \text{if } B \{ C_1 \} \text{ else } \{ C_2 \} \mid \text{while } B \text{ do } \{ C \}$

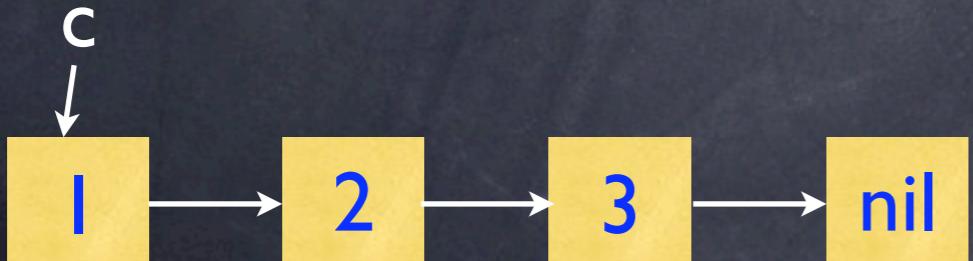
where B boolean guard $E = E, E \neq E$, etc.

Example Program: List Reversal

```
p:=nil;  
while (c !=nil) do {  
    t:=p;  
    p:=c;  
    c:=[c];  
    [p]:=t;  
}
```

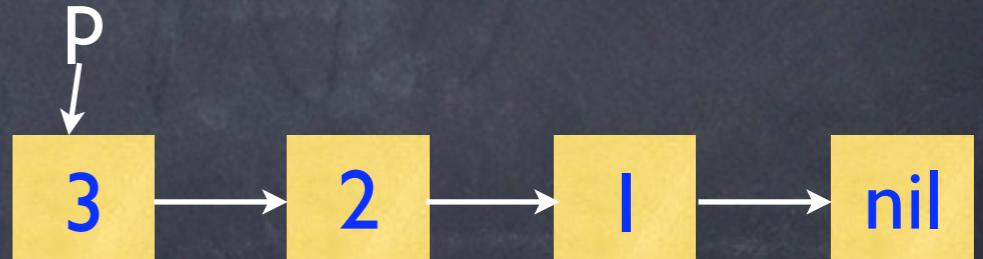
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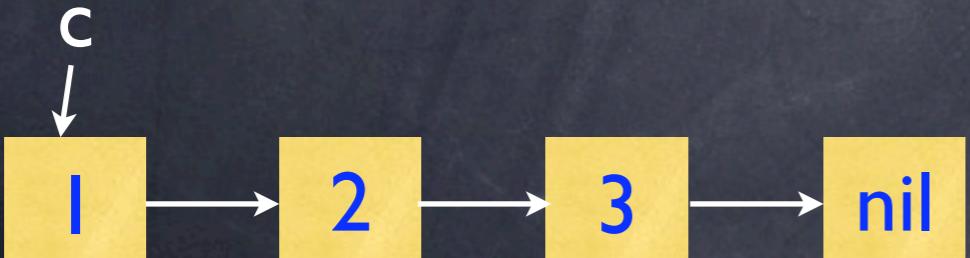
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Some properties
we would like to prove:

Does the program preserve
acyclicity/cyclicity?

Does it core-dump?

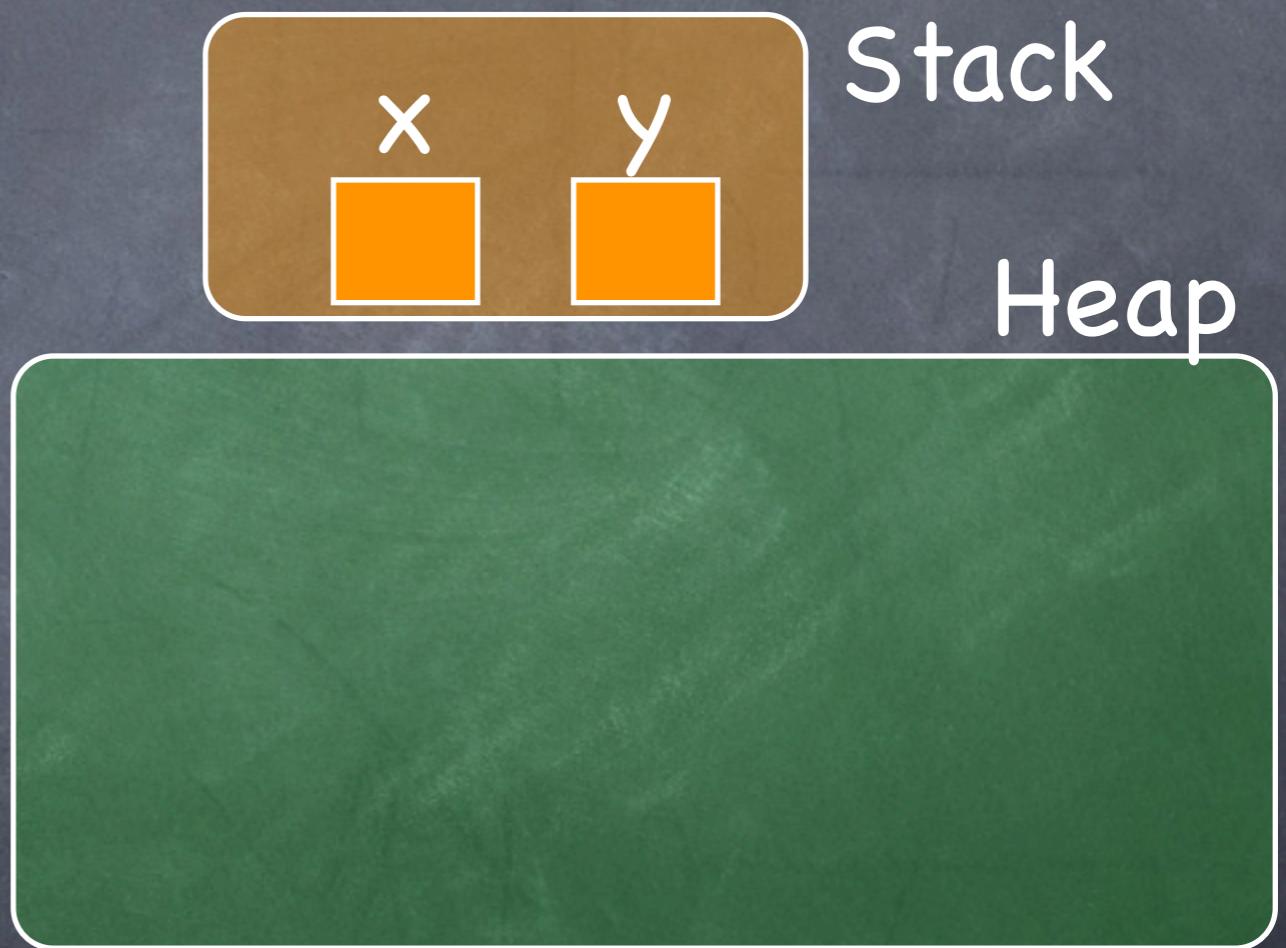
Does it create garbage?



Example Program

We are interested in pointer manipulating programs

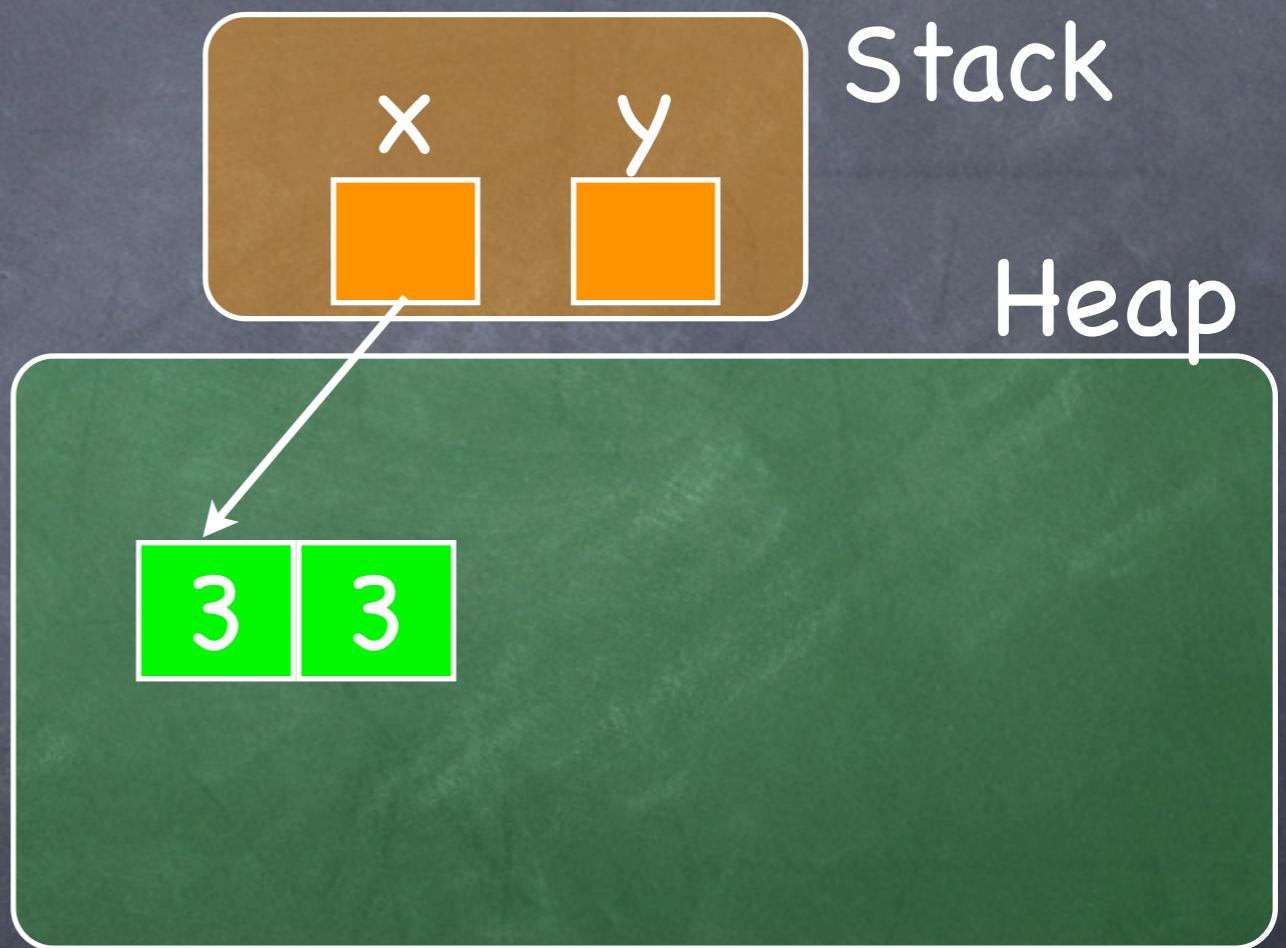
```
→ x := new(3,3);
    y := new(4,4);
    [x+1] := y;
    [y+1] := x;
    y := x+1;
    dispose x;
    y := [y];
```



Example Program

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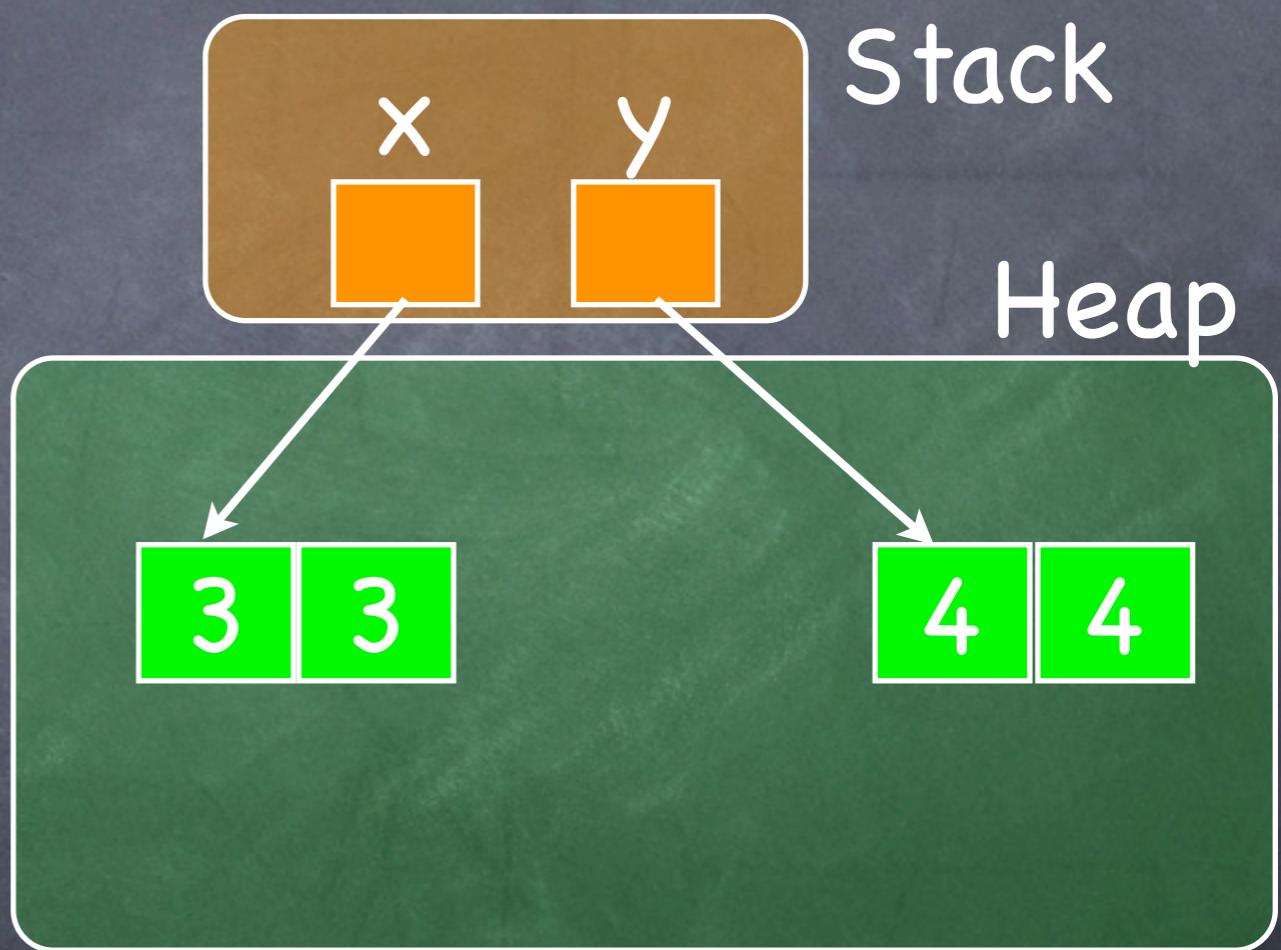
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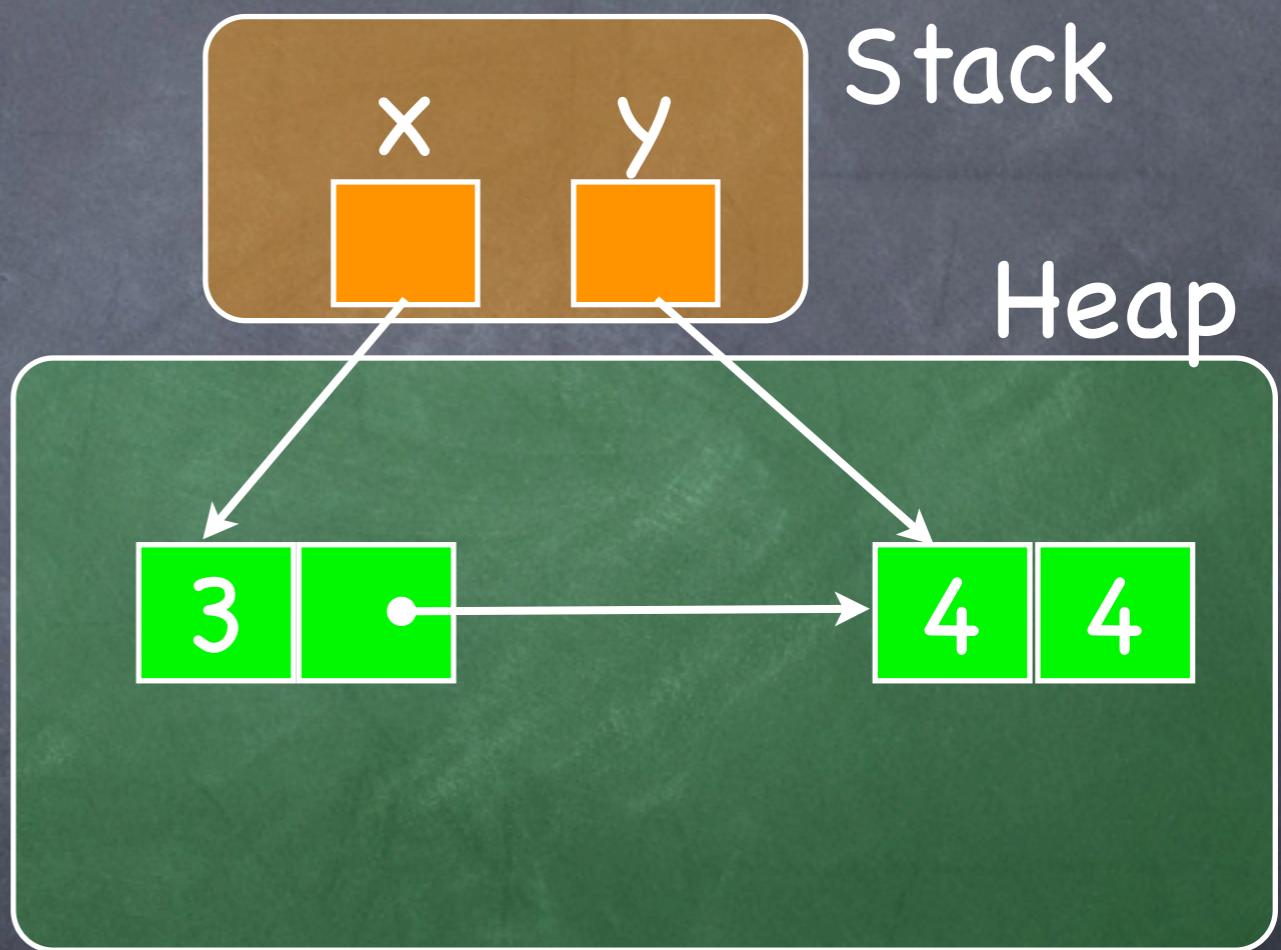
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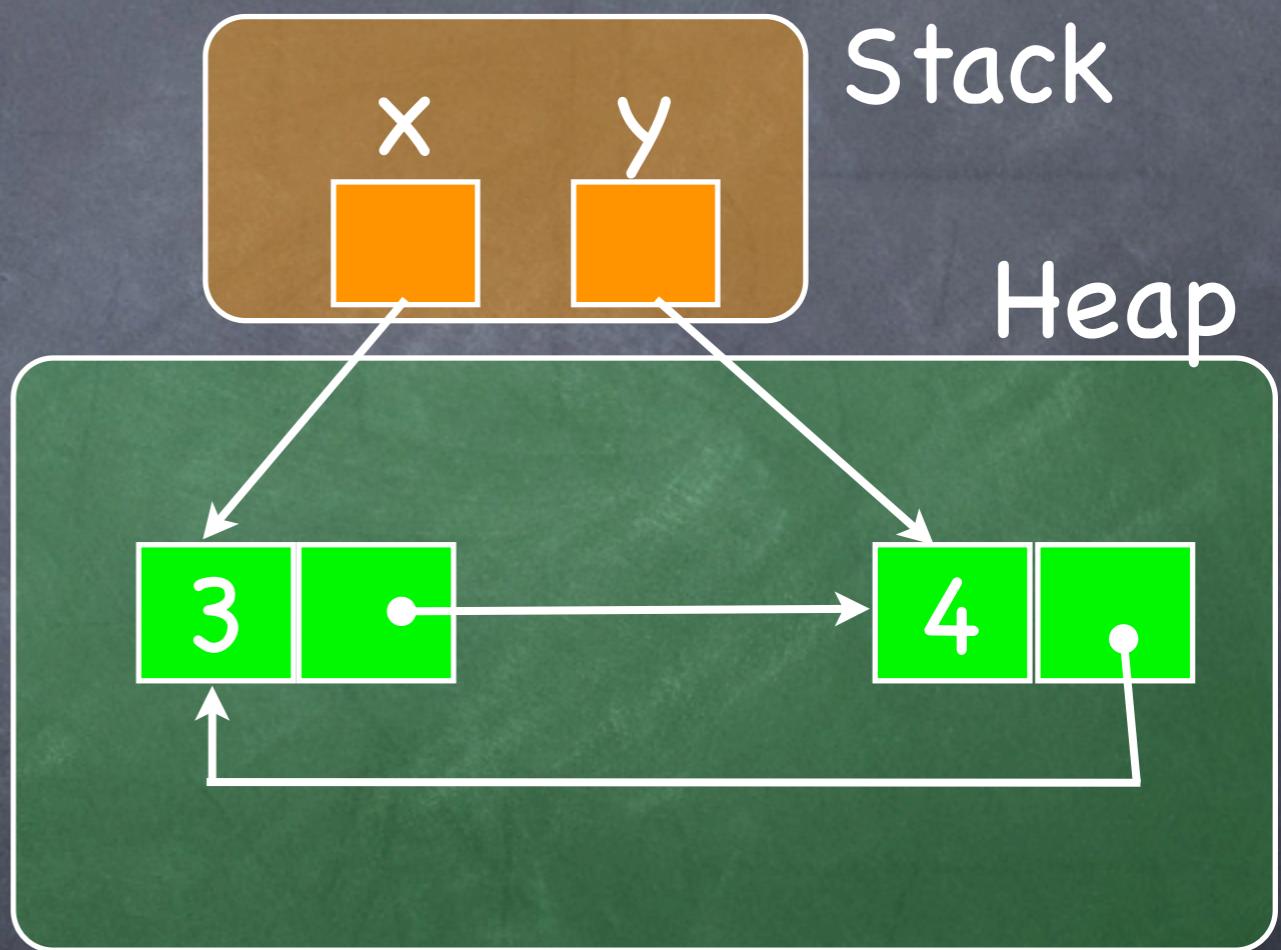
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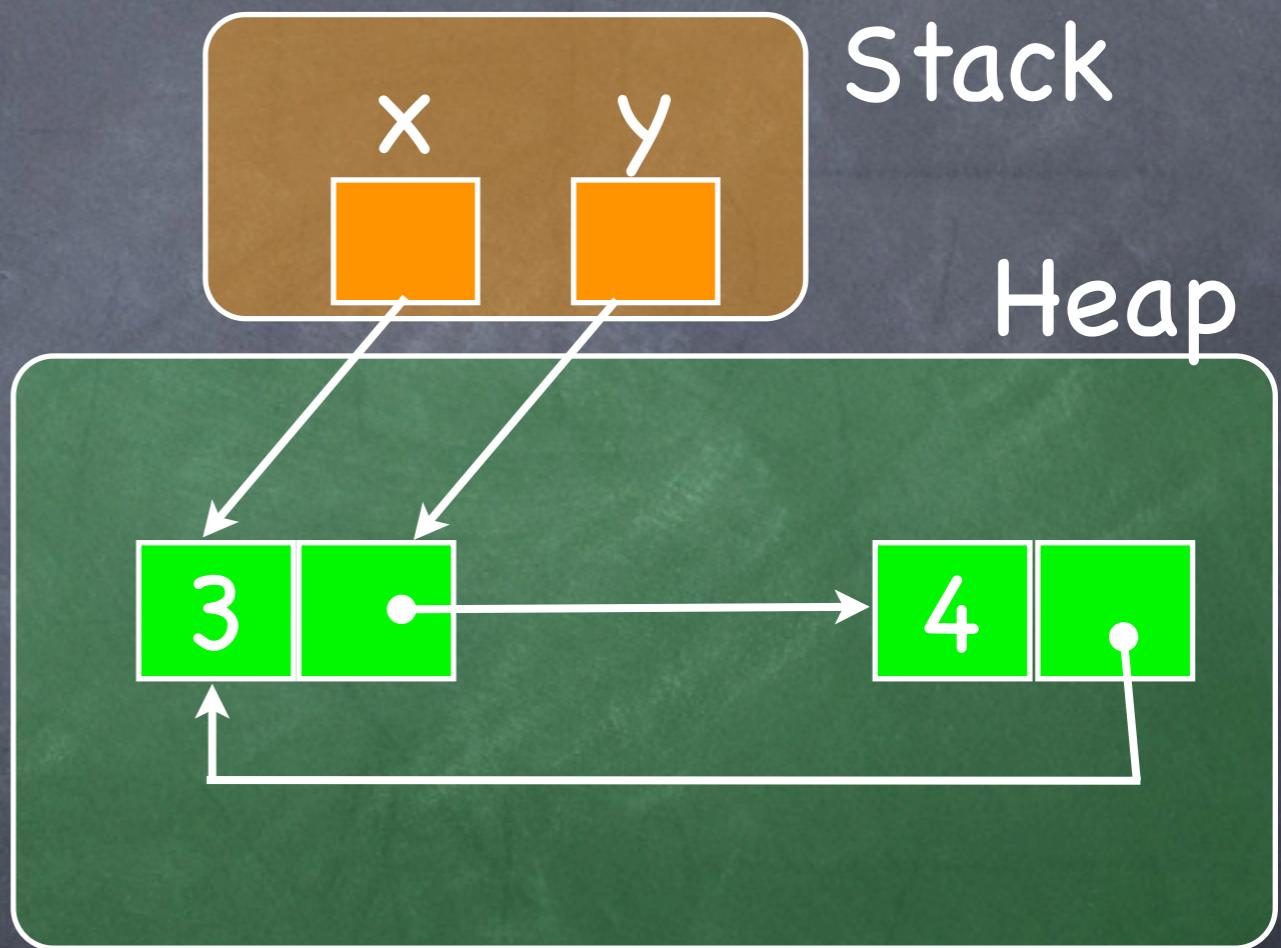
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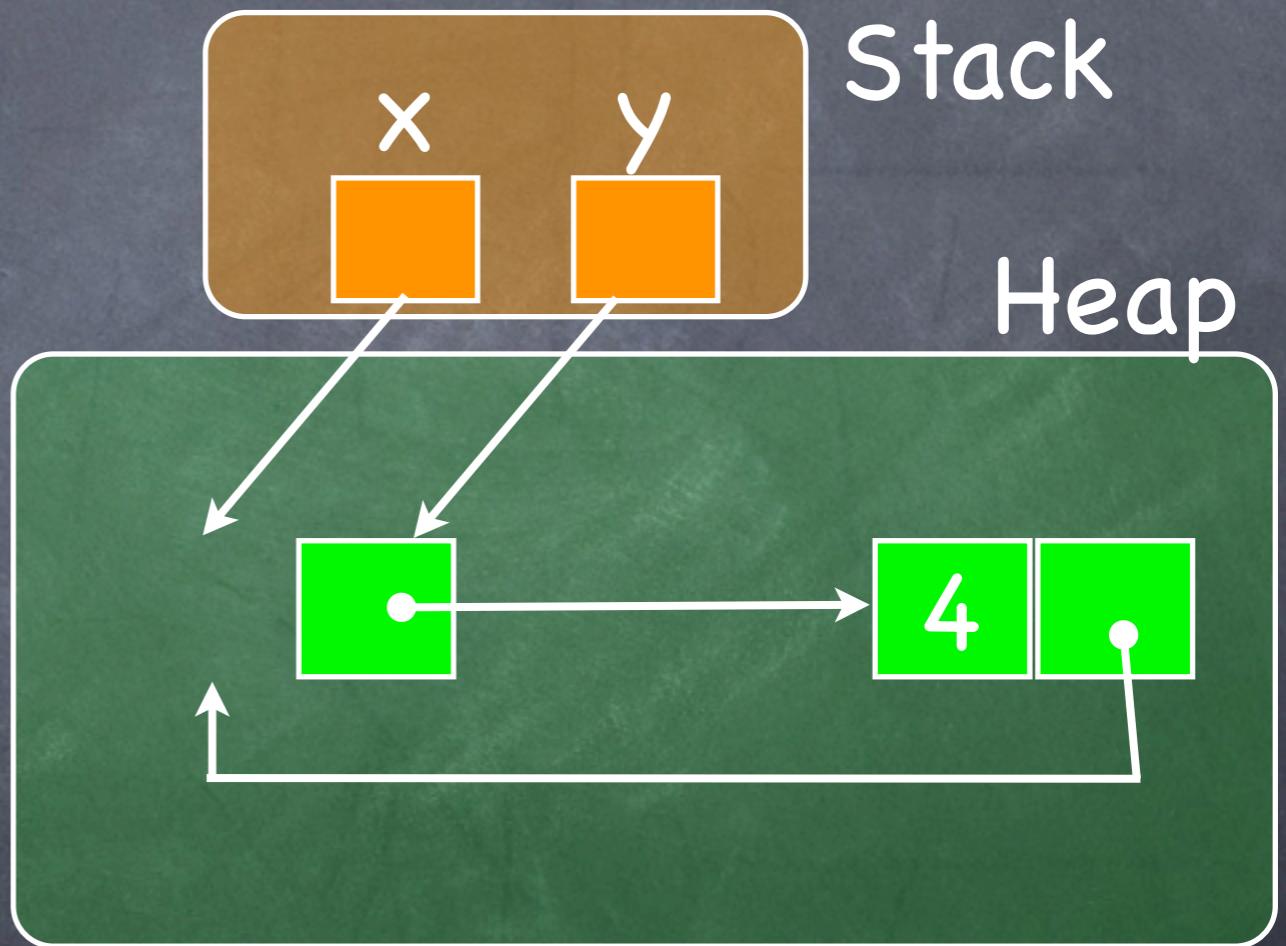
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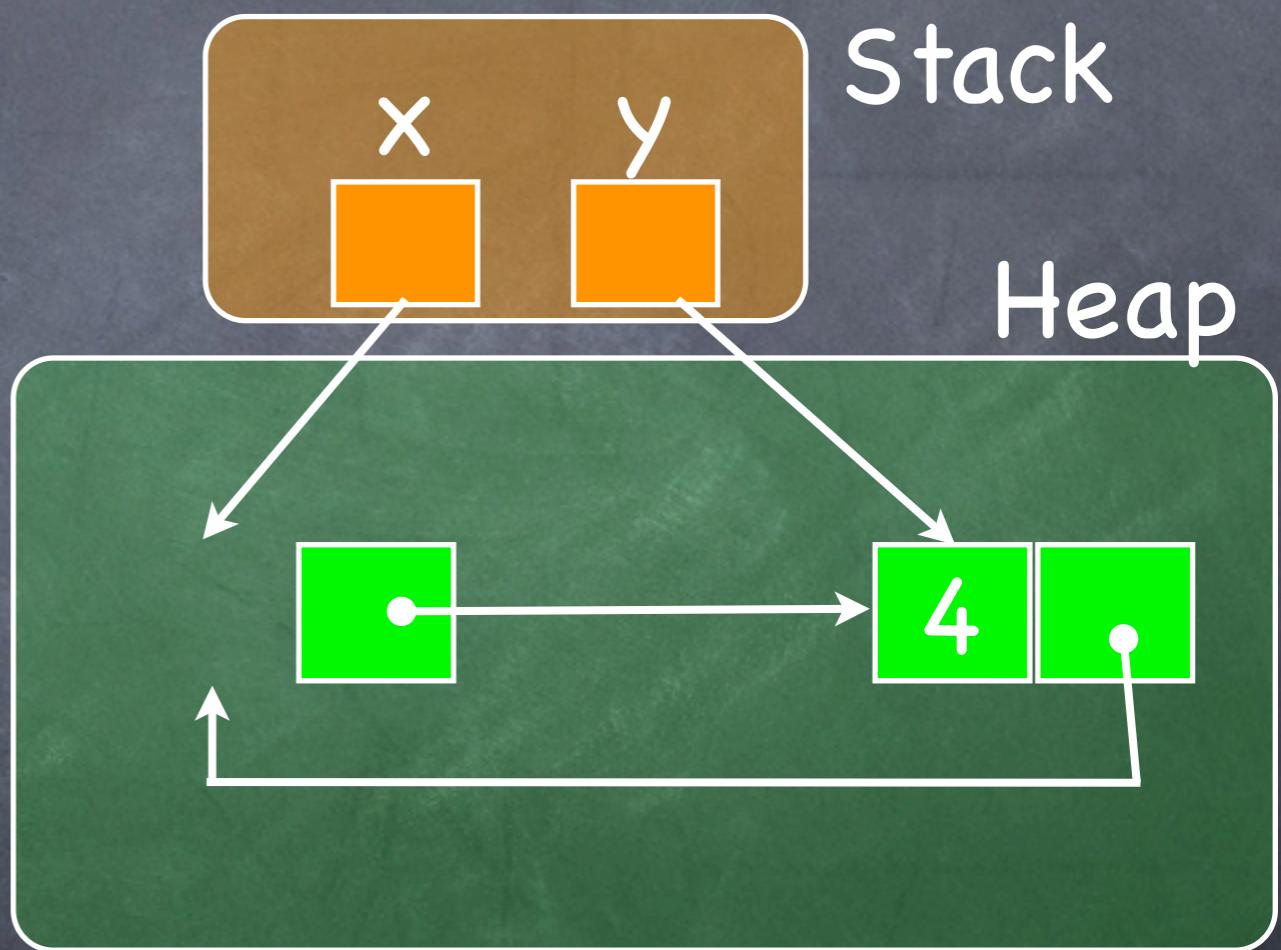
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```



Why Separation Logic?

Consider this code:

```
[y] := 4;
```

```
[z] := 5;
```

```
Guarantee([y] != [z])
```

We need to know that things are different. **How?**

Why Separation Logic?

Consider this code:

Assume($y \neq z$)

$[y] := 4;$

$[z] := 5;$

Guarantee($[y] \neq [z]$)

Add assertion?

We need to know that things are different. **How?**

Why Separation Logic?

Consider this code:

Assume($y \neq z$)

$[y] := 4;$

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Add assertion?

We need to know that things are different. How?

We need to know that things stay the same. How?

Why Separation Logic?

Consider this code:

Assume($[x] = 3$)

Assume($y \neq z$)

$[y] := 4;$

$[z] := 5;$

Add assertion?

Guarantee($[y] \neq [z]$)

Guarantee($[x] = 3$)

We need to know that things are different. How?

We need to know that things stay the same. How?

Why Separation Logic?

Consider this code:

Assume($[x] = 3 \And x \neq y \And x \neq z$) Add assertion?

Assume($y \neq z$) Add assertion?

$[y] := 4;$

$[z] := 5;$

Guarantee($[y] \neq [z]$)

Guarantee($[x] = 3$)

We need to know that things are different. How?

We need to know that things stay the same. How?

Framing

We want a general concept of things not being affected.

$$\frac{\{P\} \subset \{Q\}}{\{R \And P\} \subset \{Q \And R\}}$$

What are the conditions on C and R?

Hard to define if reasoning about a heap and aliasing

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What are the conditions on C and R?

Hard to define if reasoning about a heap and aliasing

This is where separation logic comes in

$$\frac{\{P\} \subset \{Q\}}{\{R * P\} \subset \{Q * R\}}$$

Introduces new connective $*$ used to separate state.

Storage Model

$$\begin{aligned} \text{Vars} &\stackrel{\text{def}}{=} \{x, y, z, \dots\} \\ \text{Locs} &\stackrel{\text{def}}{=} \{1, 2, 3, 4, \dots\} & \text{Vals} &\supseteq \text{Locs} \end{aligned}$$

$$\begin{aligned} \text{Heaps} &\stackrel{\text{def}}{=} \text{Locs} \rightarrow_{\text{fin}} \text{Vals} \\ \text{Stacks} &\stackrel{\text{def}}{=} \text{Vars} \rightarrow \text{Vals} \\ \text{States} &\stackrel{\text{def}}{=} \text{Stacks} \times \text{Heaps} \end{aligned}$$

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Stack

x 7

y 42

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Heap

7
0

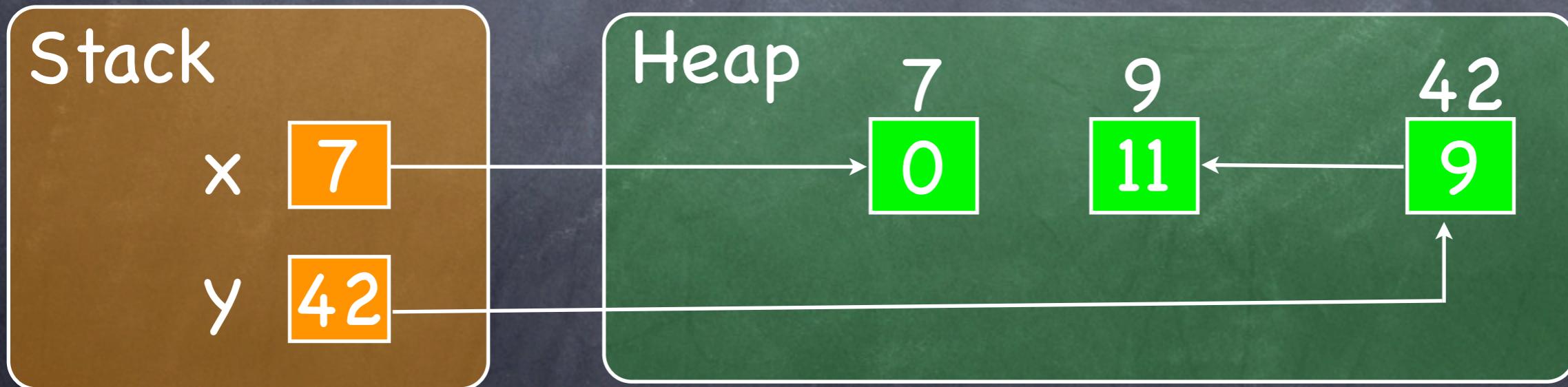
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11

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Assertions

$$\begin{array}{lcl} E, F & ::= & x \mid n \mid E+F \mid -E \mid \dots \\ P, Q & ::= & E = F \mid E \geq F \mid E \mapsto F \\ & | & \text{emp} \mid P * Q \\ & | & \text{true} \mid P \wedge Q \mid \neg P \mid \forall x. P \end{array}$$

Heap-independent Exprs
Atomic Predicates
Separating Connectives
Classical Logic

Informal Meaning

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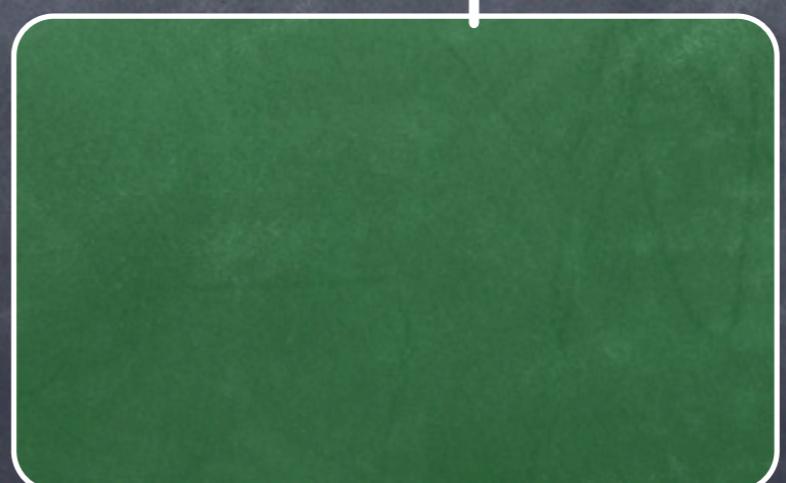
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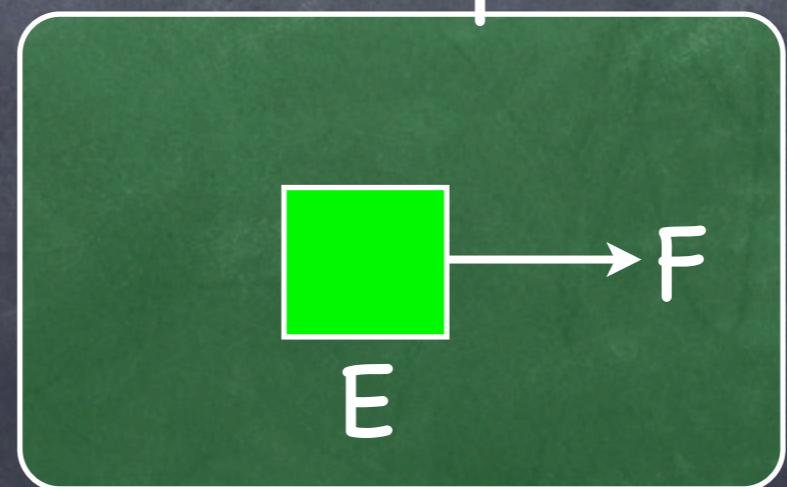
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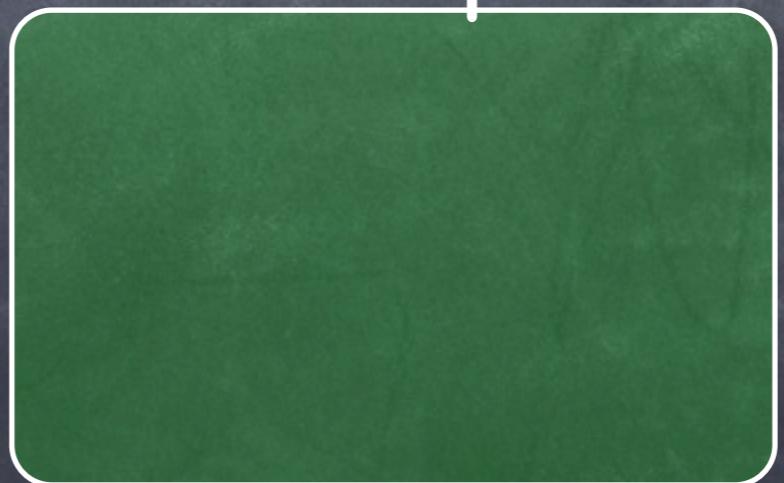
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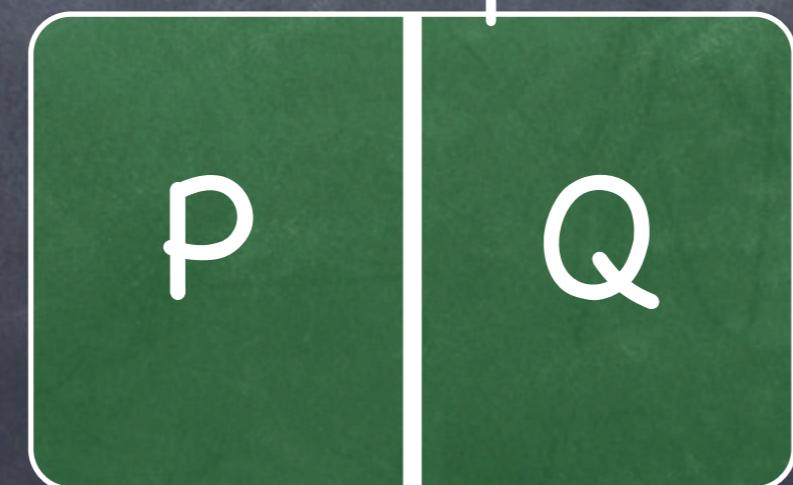
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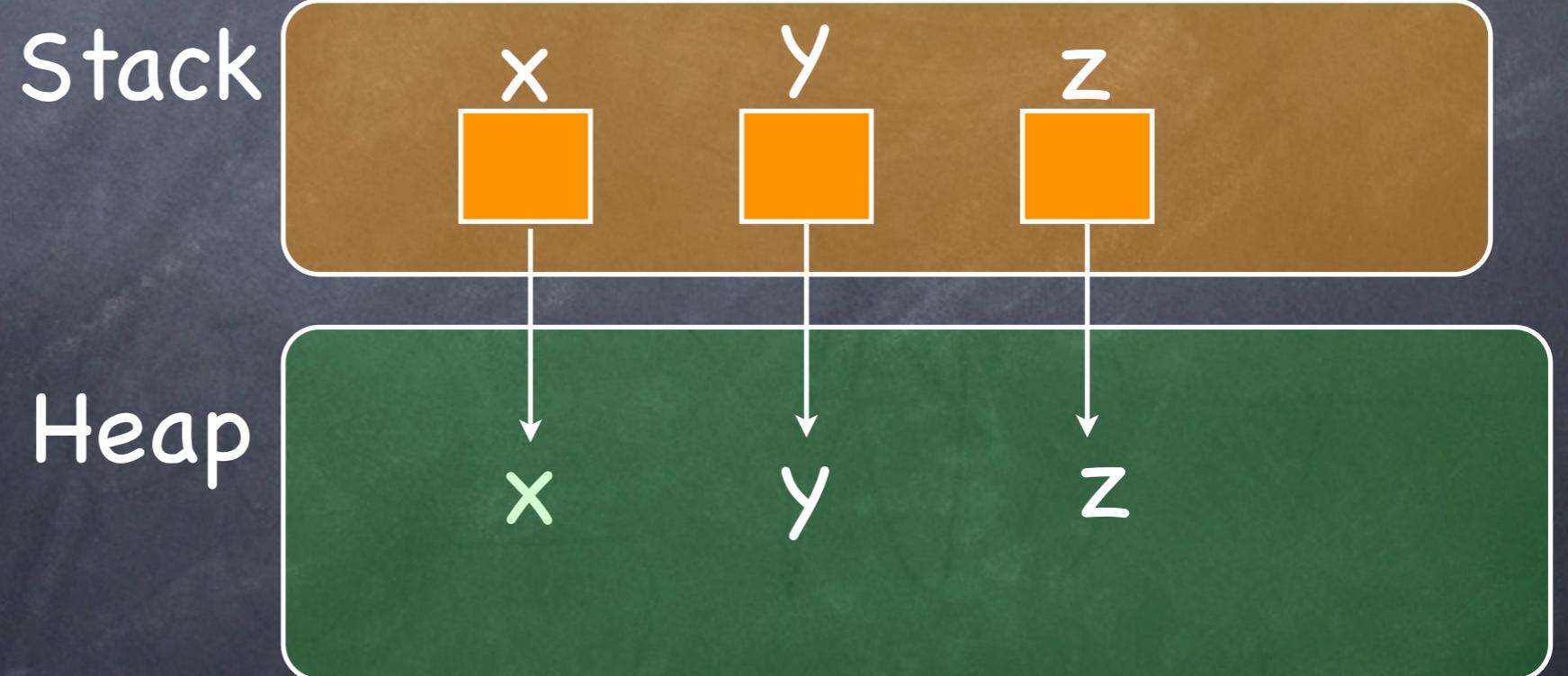
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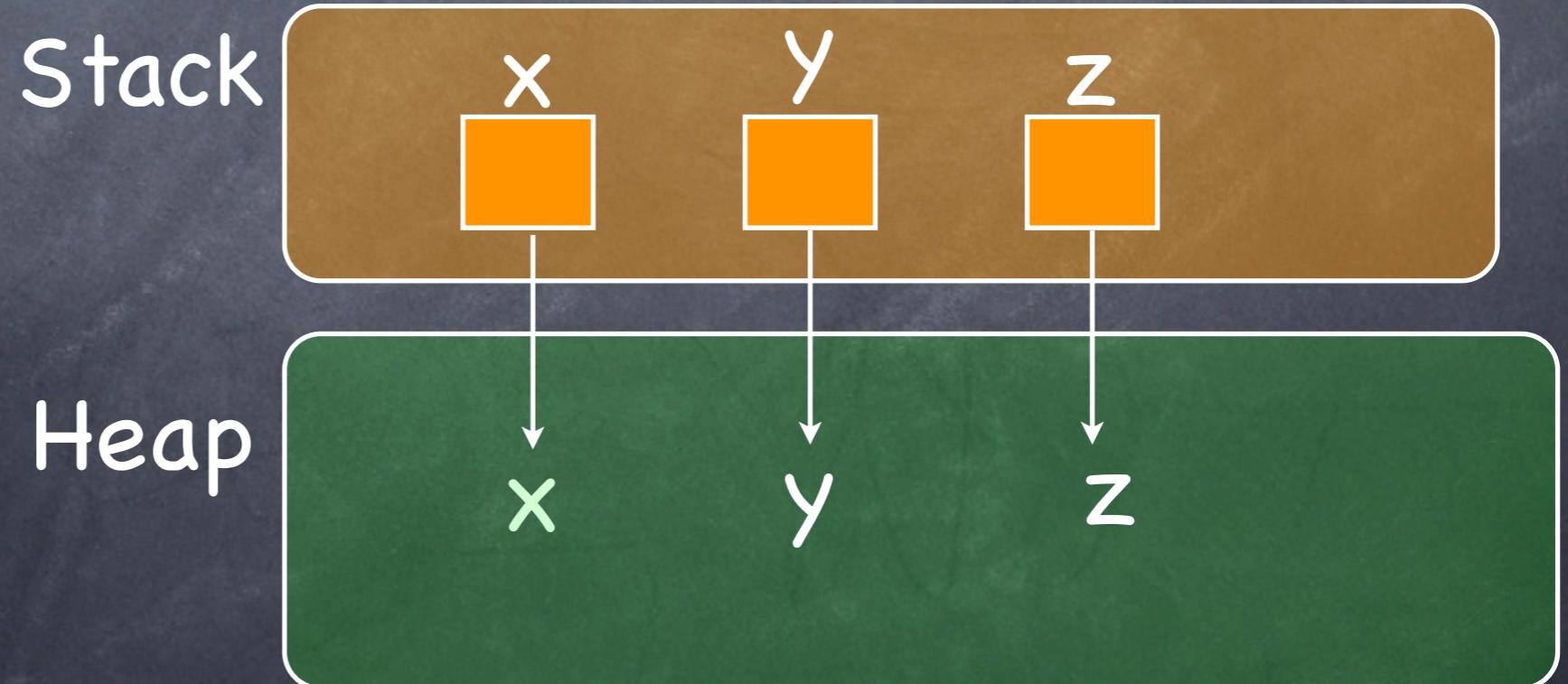
Examples

Formula: emp



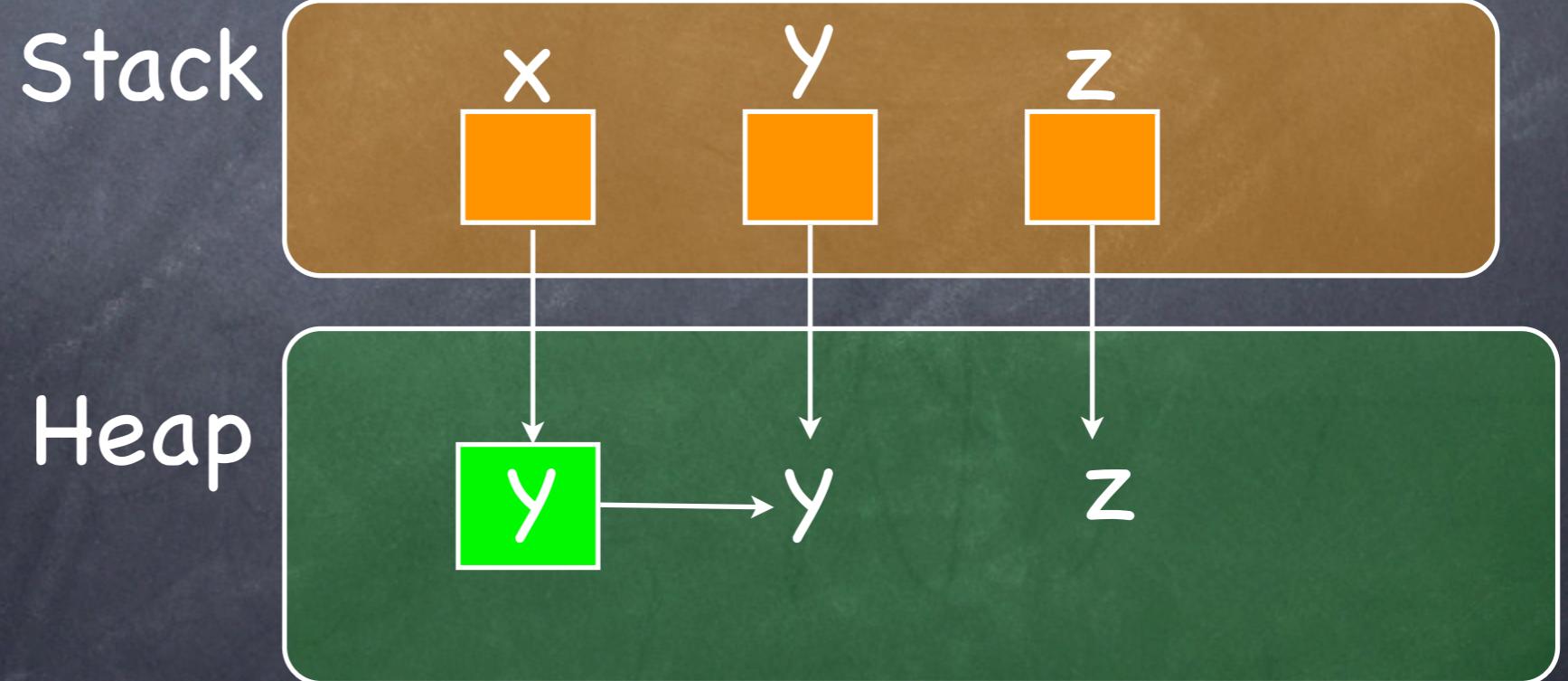
Examples

Formula: $\text{emp}^* x | \rightarrow y$



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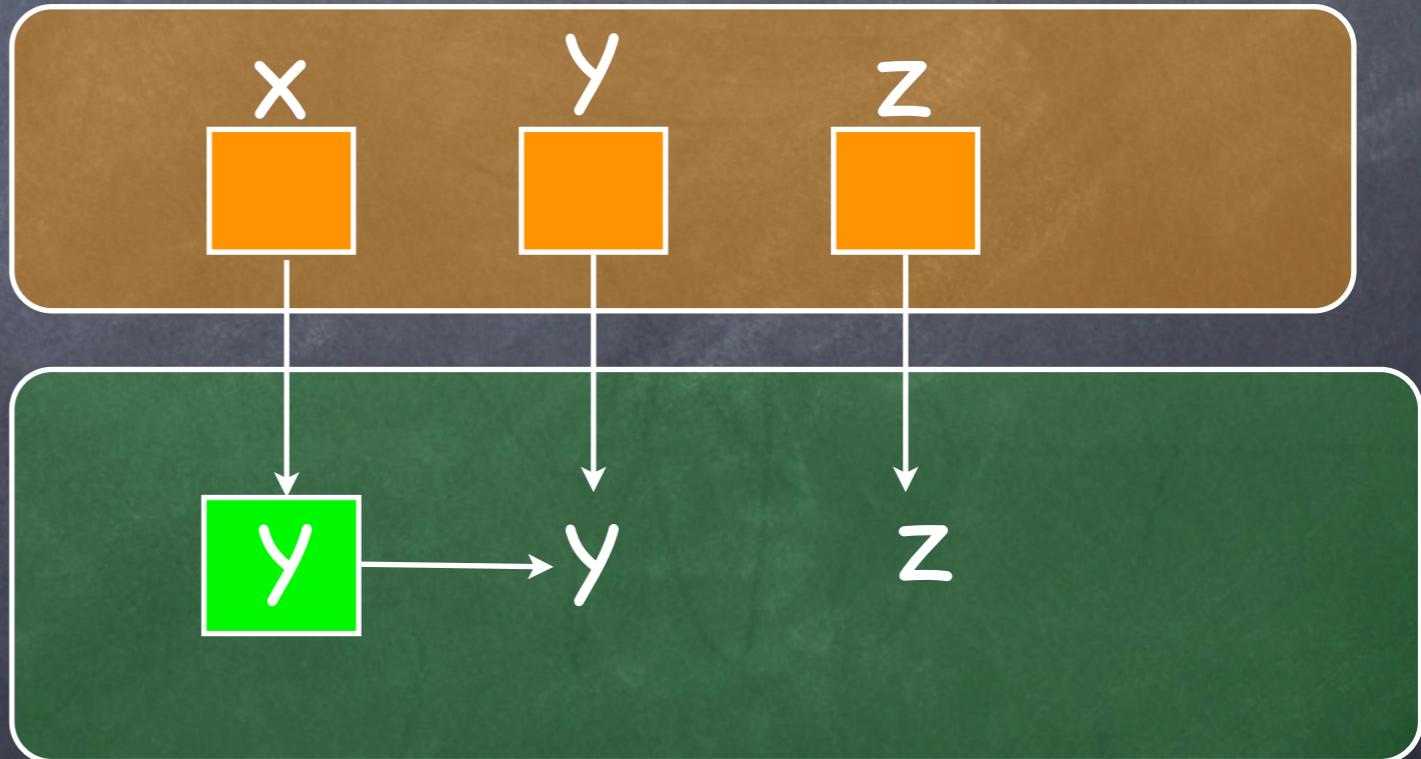


Examples

Formula:

$x|-\rightarrow y$

Stack



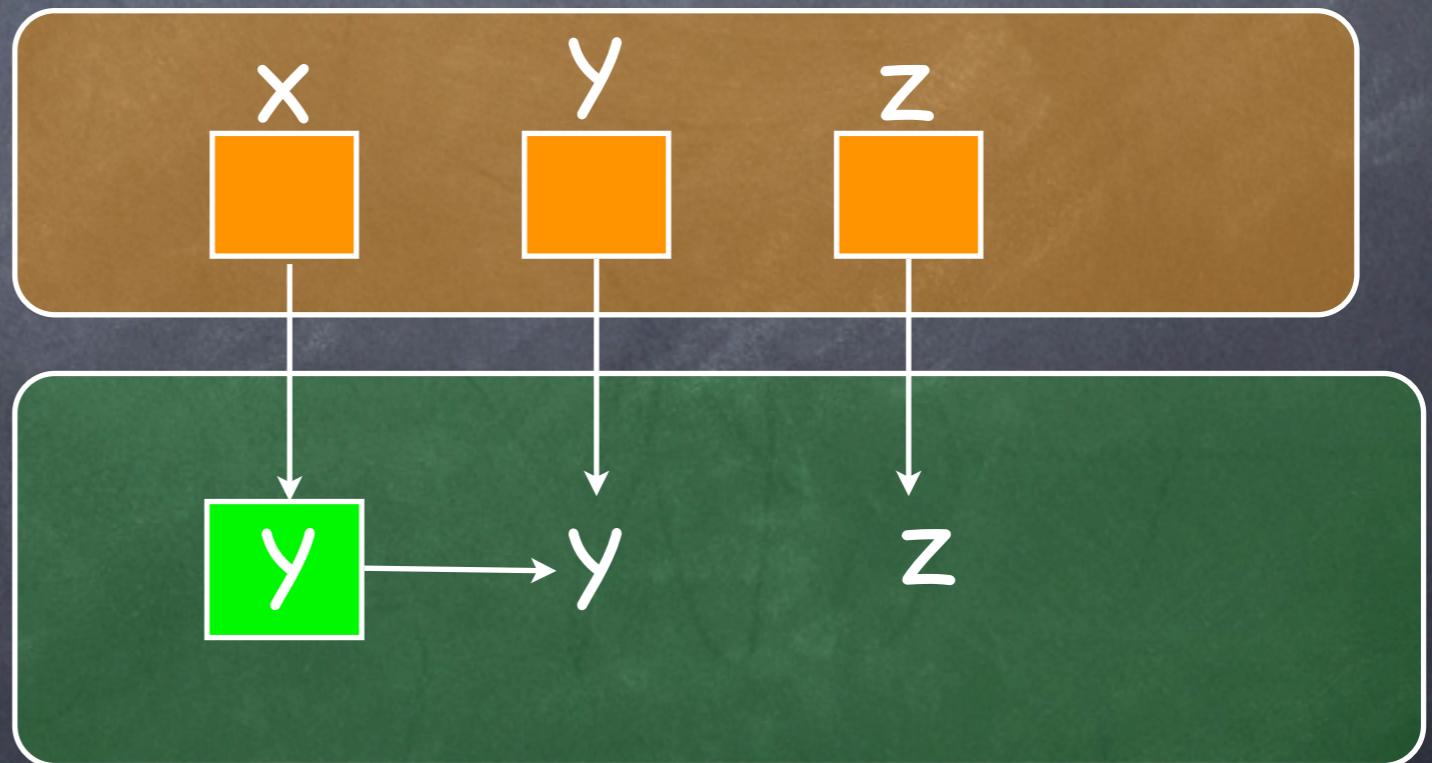
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Formula:

$x|-\>y * y|-\>z$

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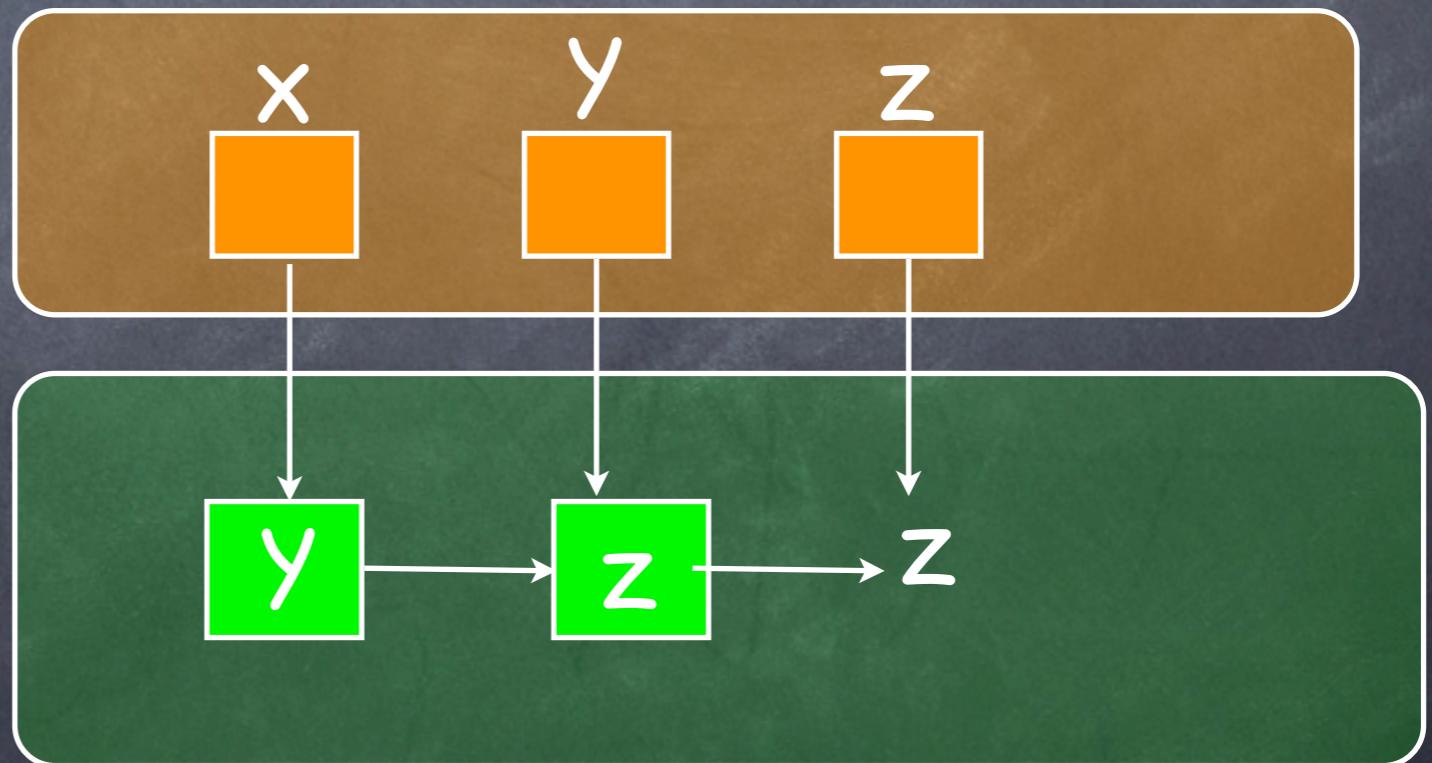
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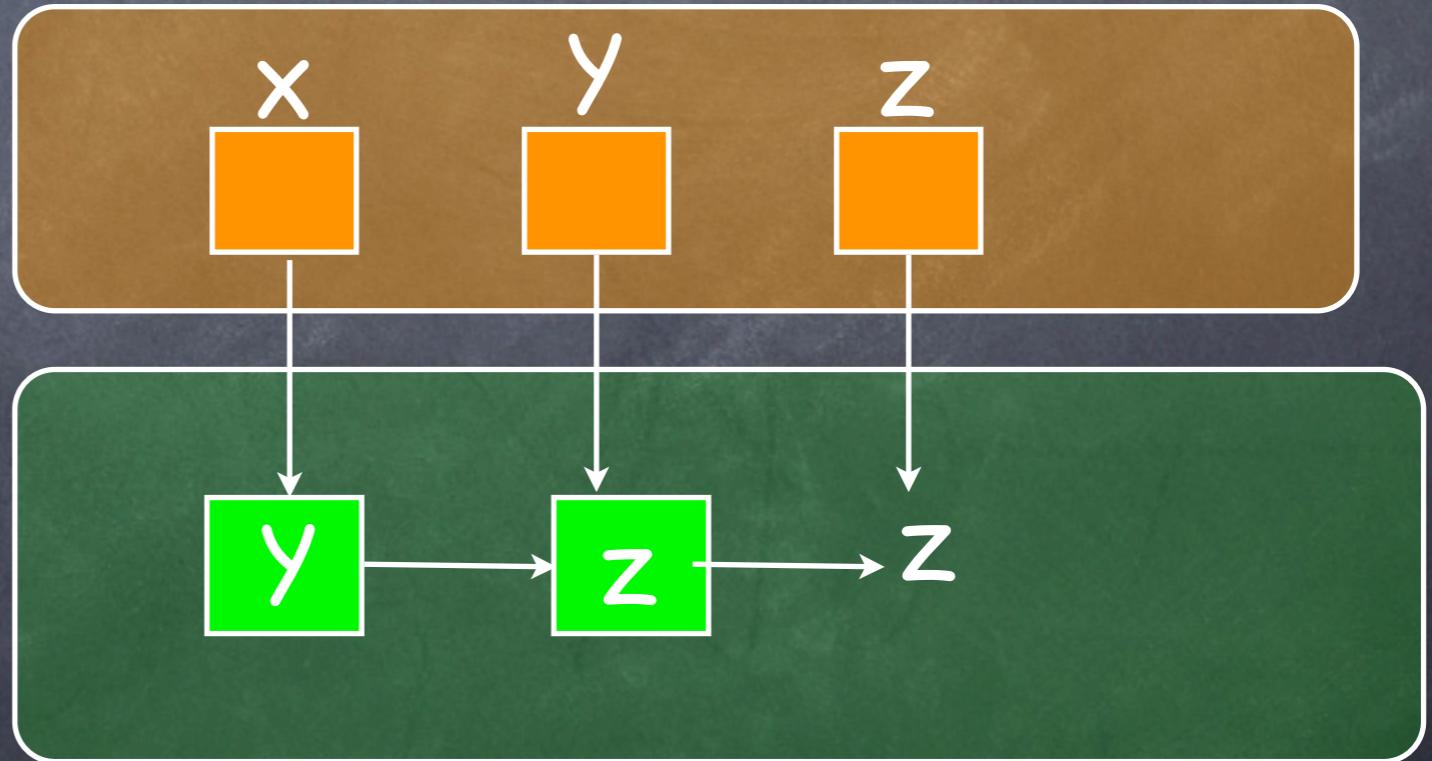
Heap

Examples

Formula:

$$x \rightarrow y * y \rightarrow z * z \rightarrow x$$

Stack



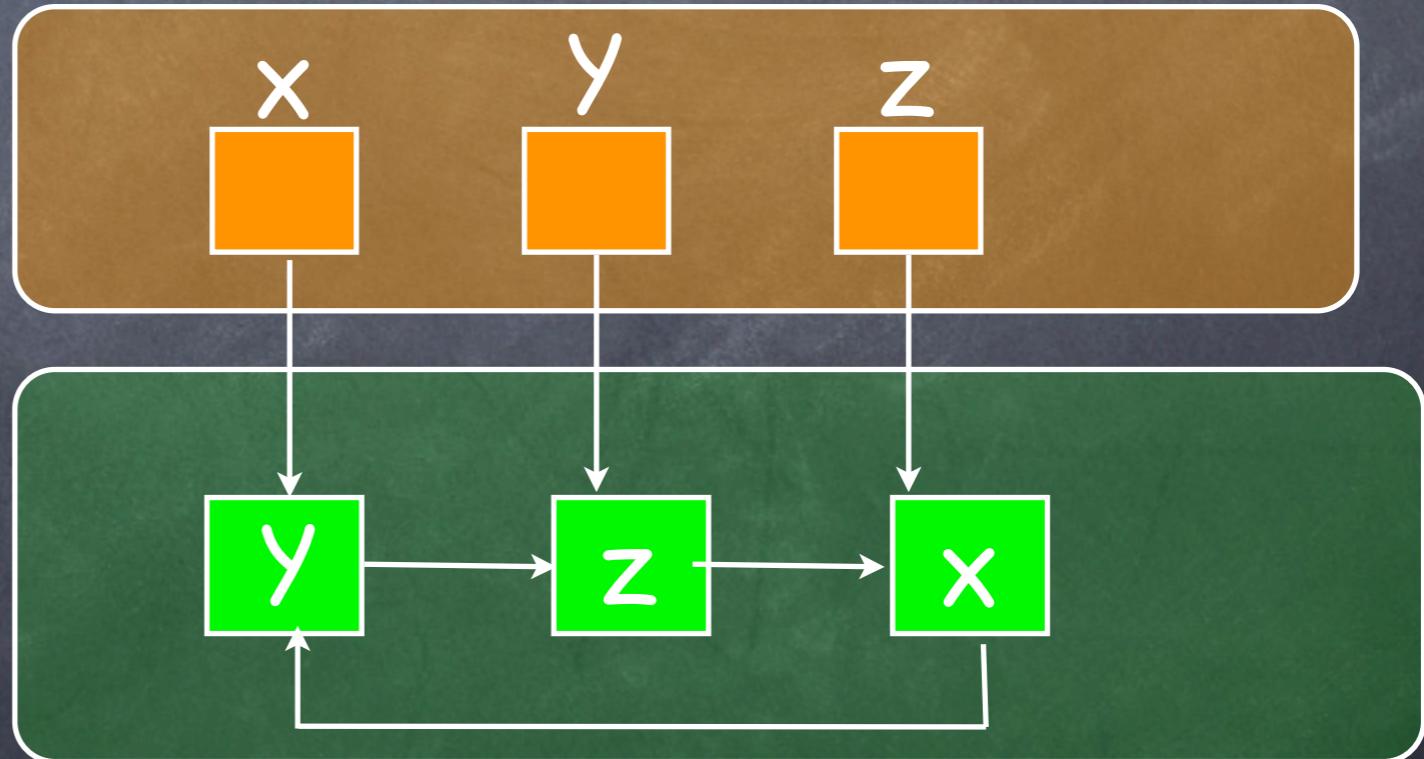
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Heap

Semantics of Assertions

$$(s, h) \models P$$

$s, h \models E \mapsto F$ iff $\text{dom}(h) = \{\llbracket E \rrbracket_s\}$ and $h(\llbracket E \rrbracket_s) = \llbracket F \rrbracket_s$

$s, h \models \text{emp}$ iff $\text{dom}(h) = \emptyset$

$s, h \models P * Q$ iff $\exists h_0, h_1. \text{dom}(h_0) \cap \text{dom}(h_1) = \emptyset$ and $h_0 \cdot h_1 = h$
and $s, h_0 \models P$ and $s, h_1 \models Q$

$s, h \models P \wedge Q$ iff $s, h \models P$ and $s, h \models Q$

where meaning of expressions

$\llbracket E \rrbracket : \text{Stacks} \rightarrow \text{Vals}$

Example

Stack

Heap

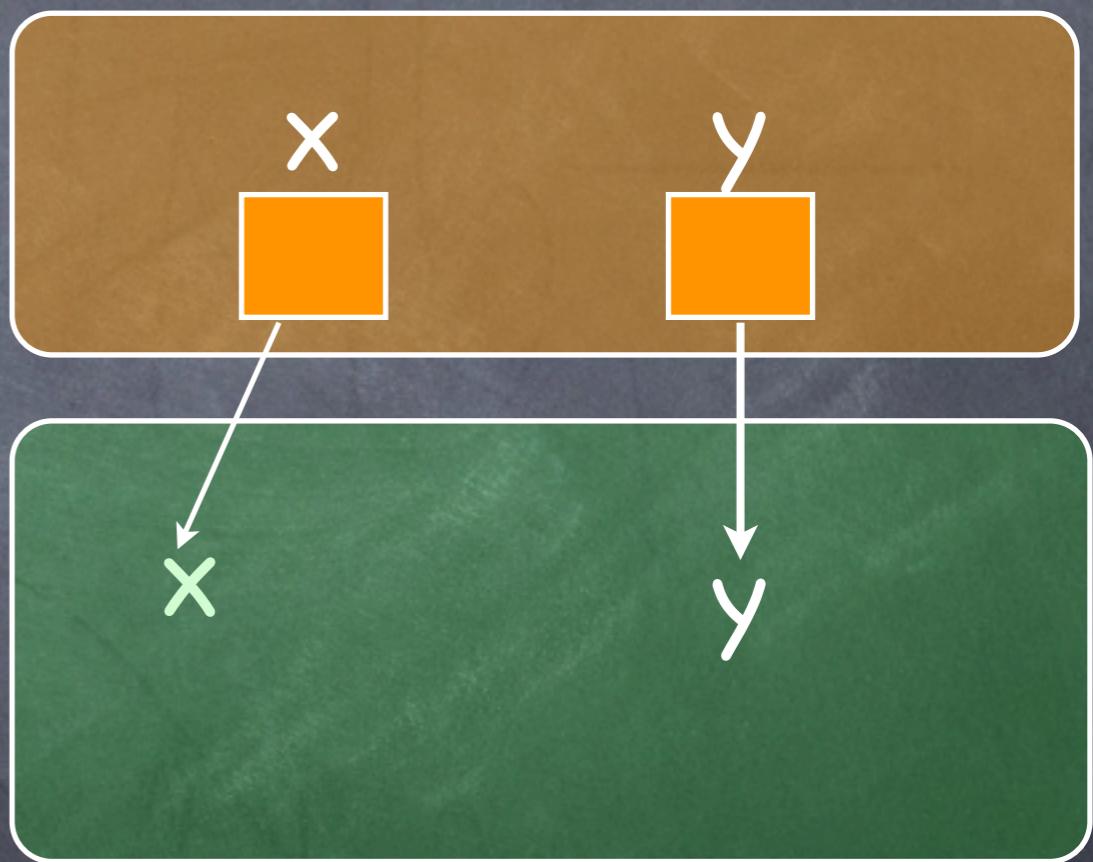
Abbreviation: E points to a record of
several fields: $E \mapsto E_1, \dots, E_n \triangleq E \mapsto E_1 * \dots * E + n - 1 \mapsto E_n$

Example

$x \mapsto 3, y$

Stack

Heap



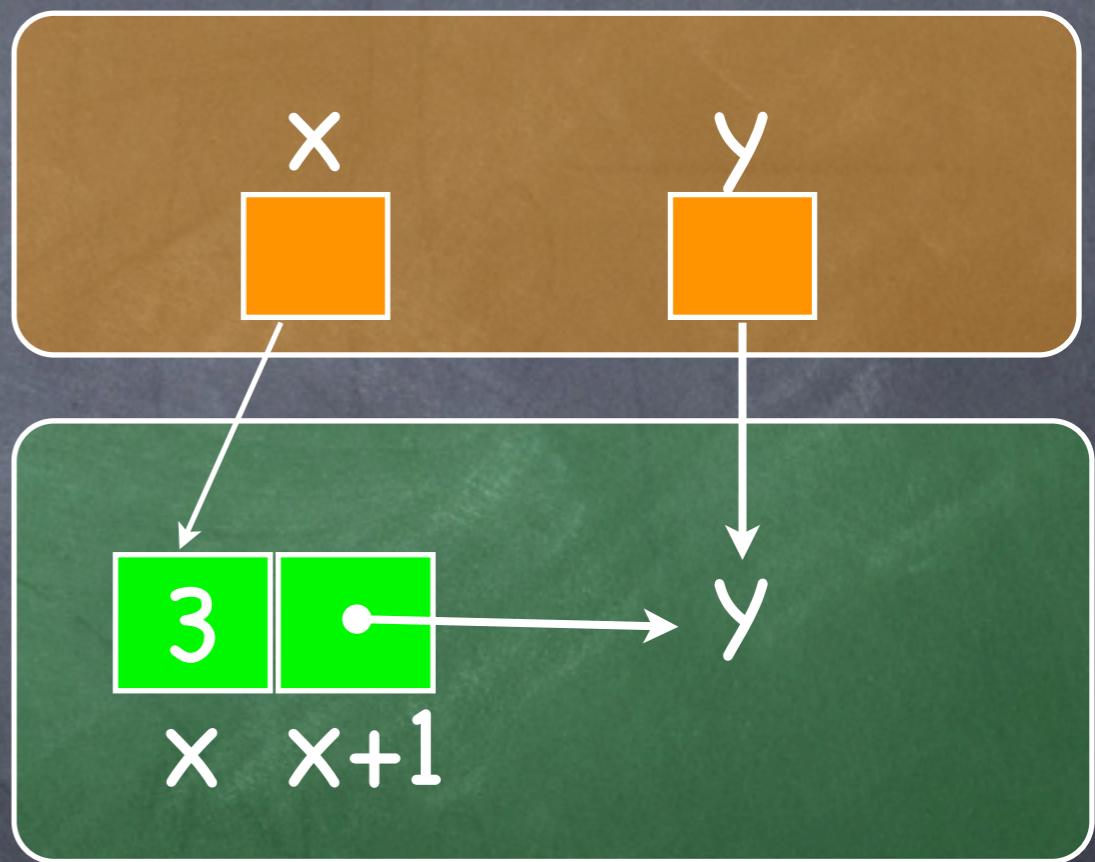
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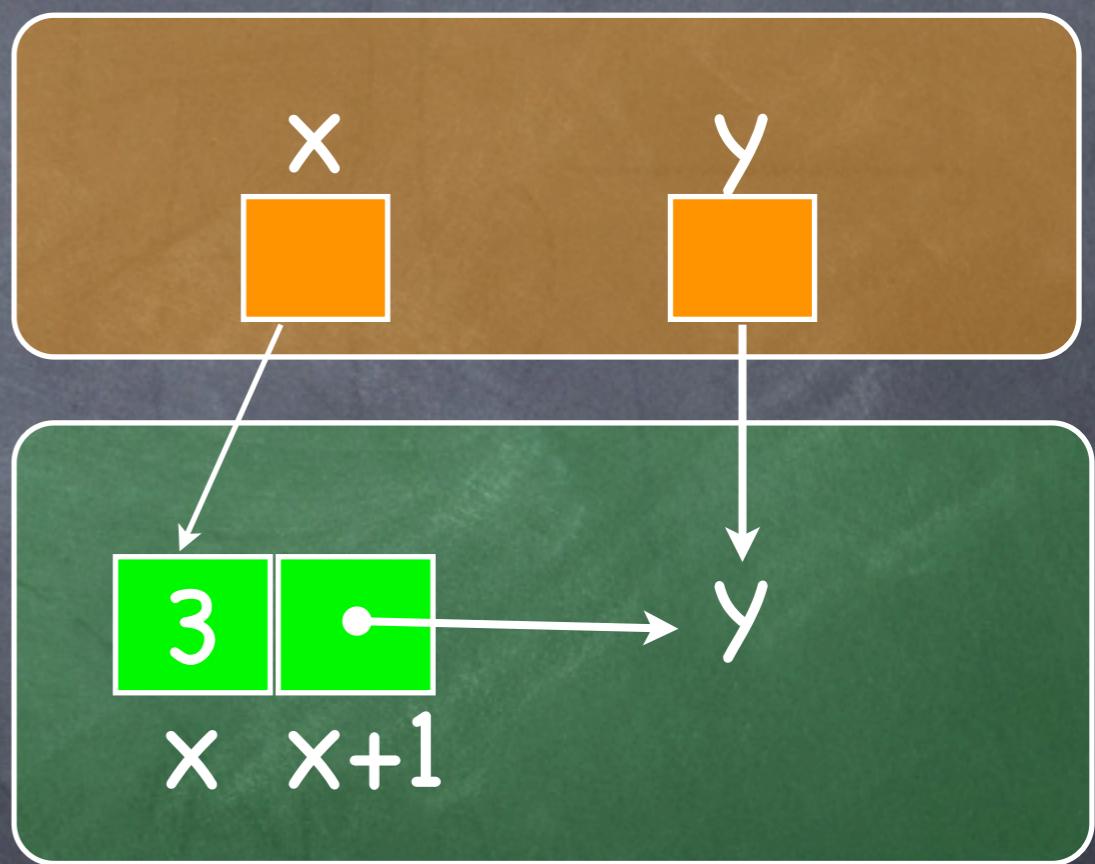
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$y \mapsto 3, x$

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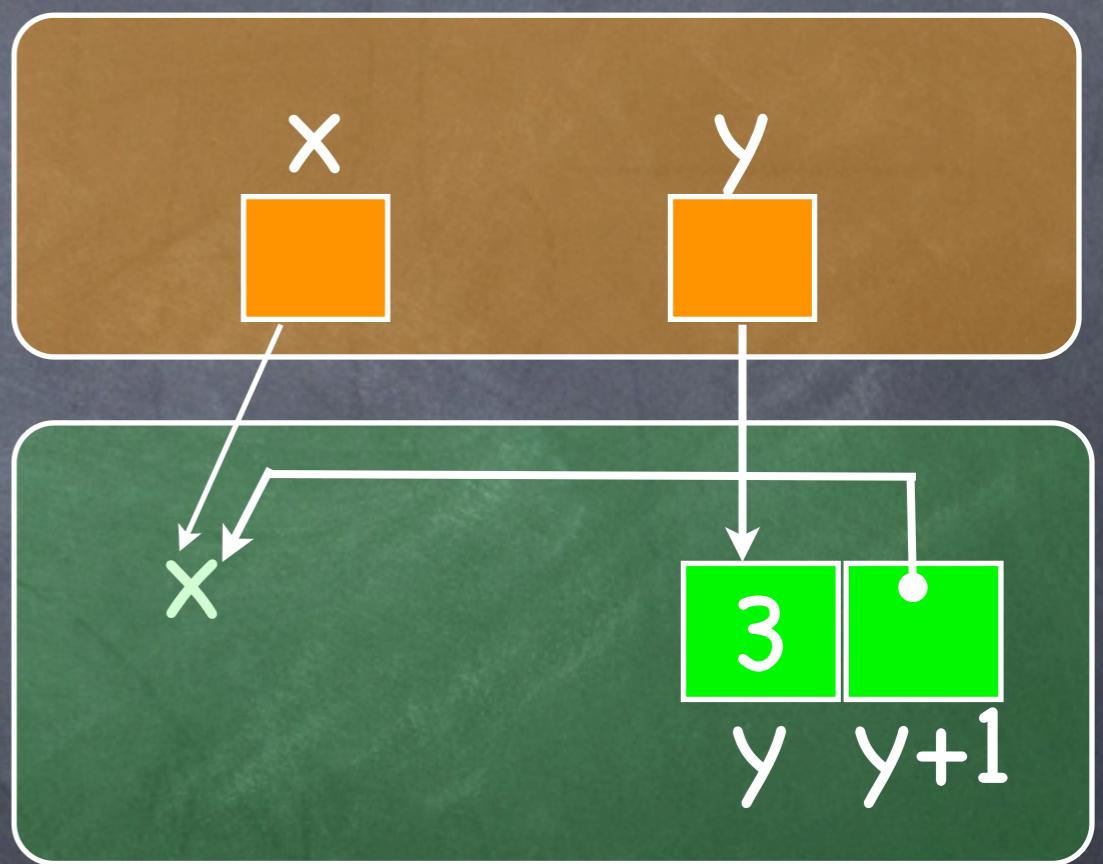
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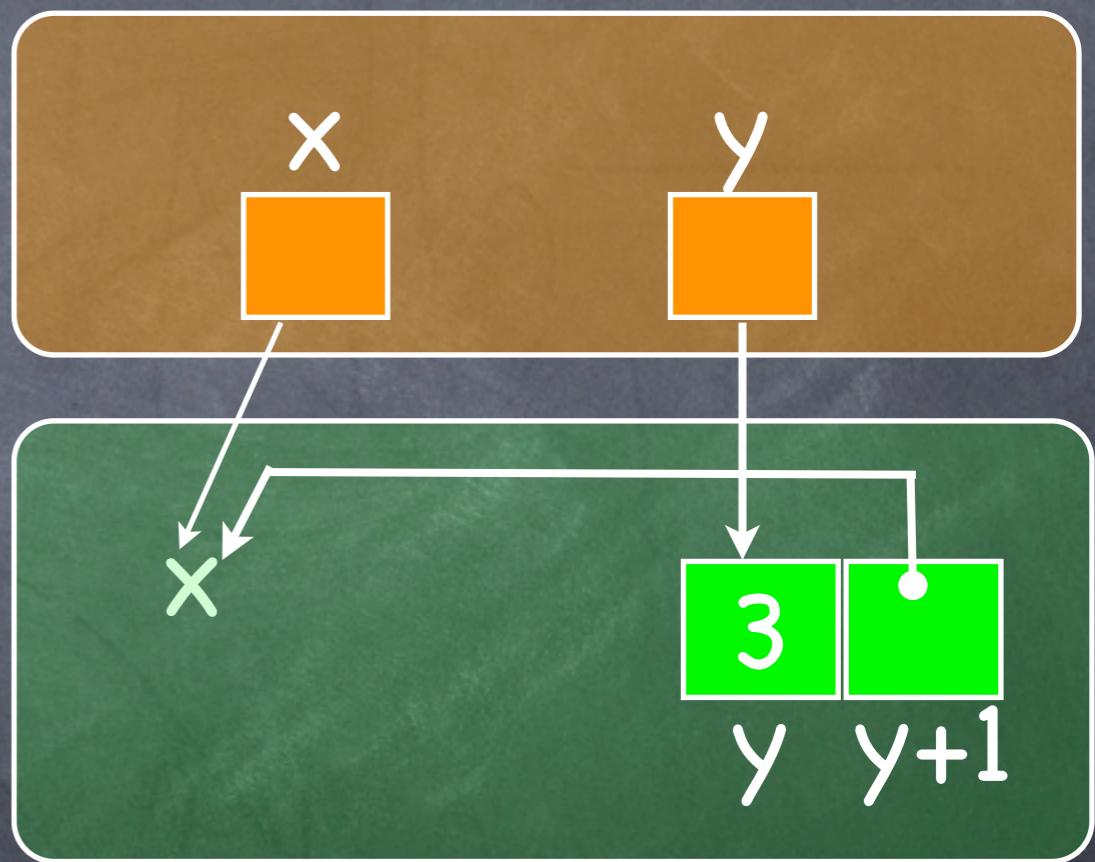
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$x \mapsto 3, y * y \mapsto 3, x$

Stack

Heap



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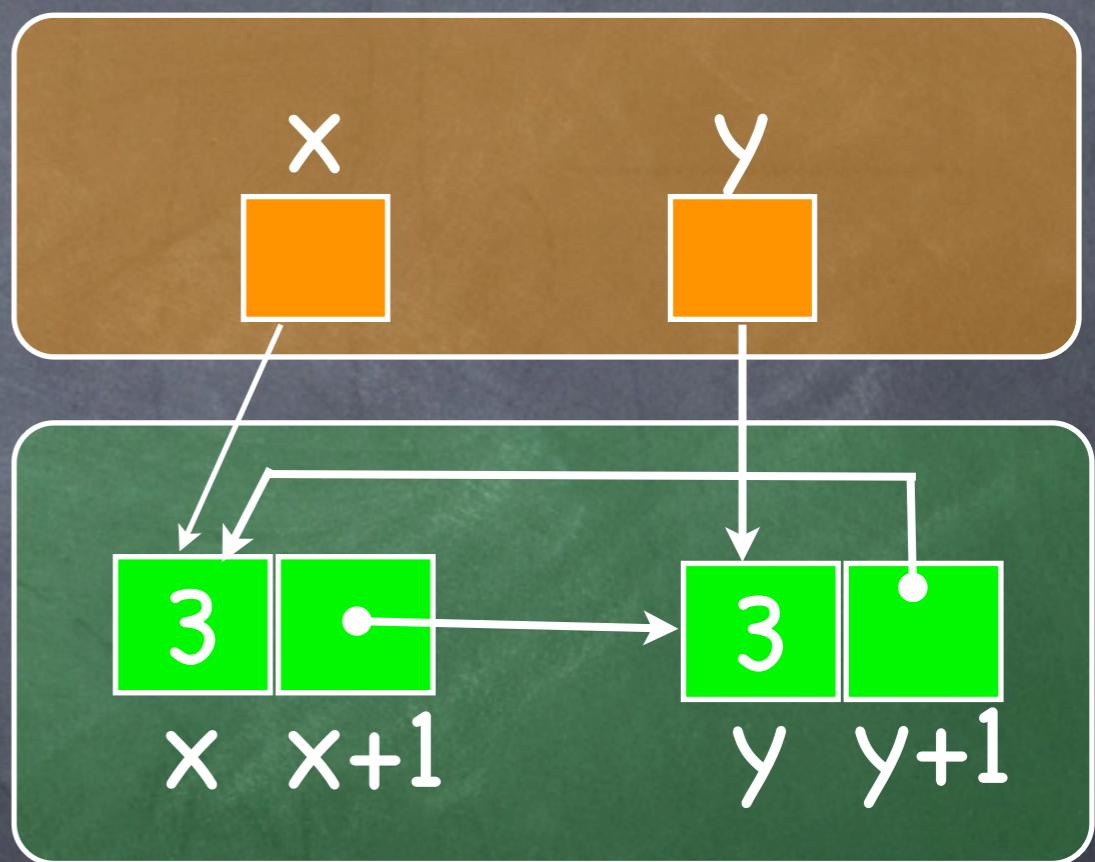
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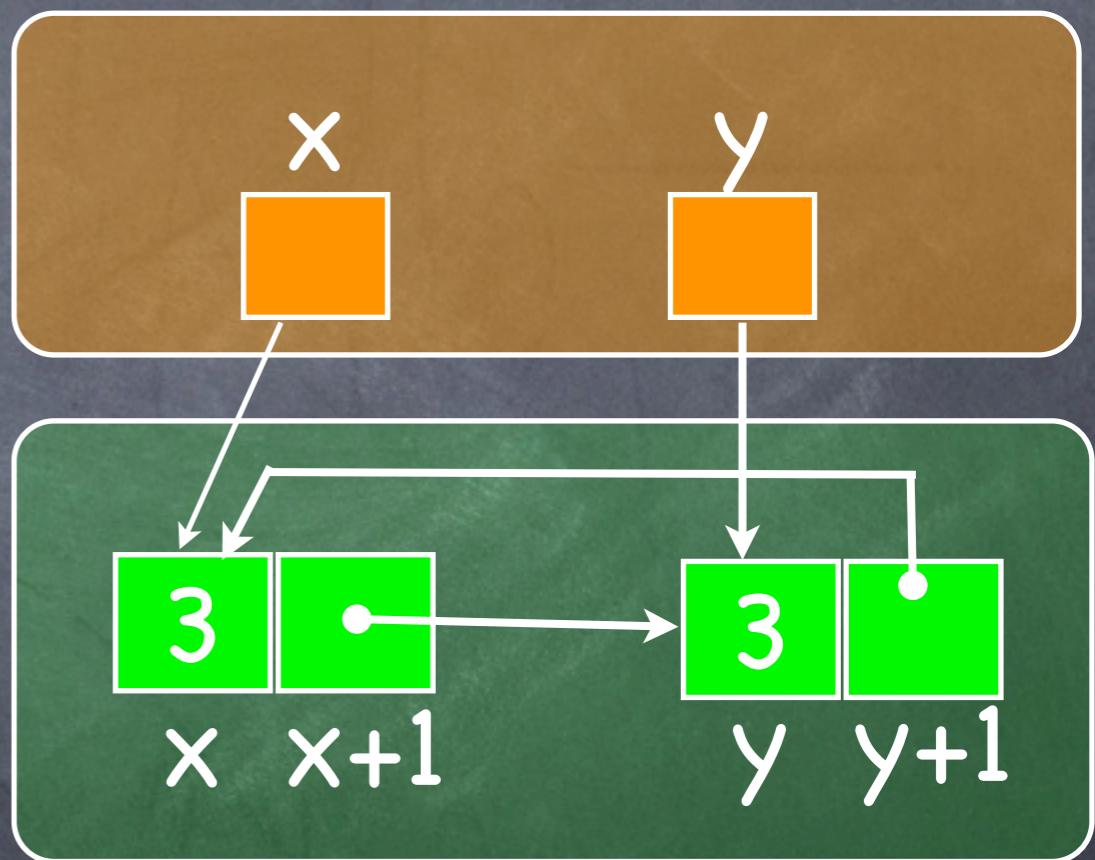
$y \mapsto 3, x$

$x \mapsto 3, y * y \mapsto 3, x$

$x \mapsto 3, y \wedge y \mapsto 3, x$

Stack

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Example

$x \mapsto 3, y$

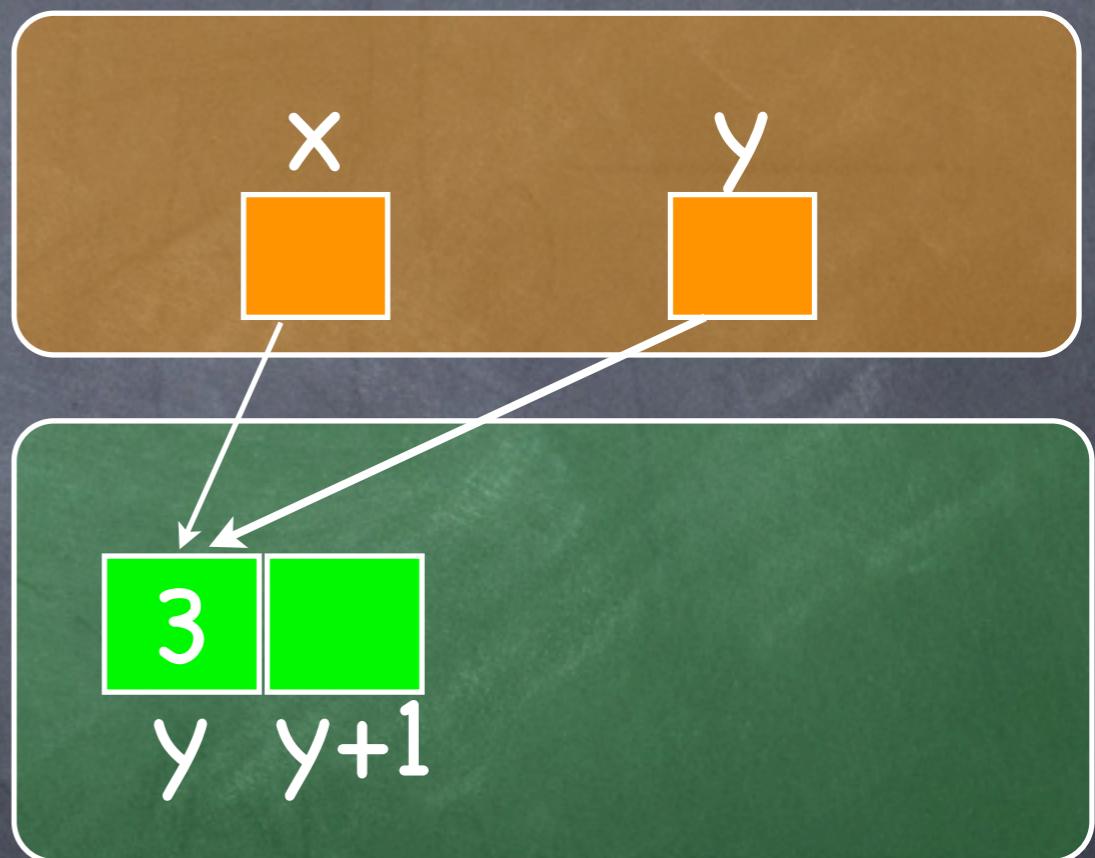
$y \mapsto 3, x$

$x \mapsto 3, y * y \mapsto 3, x$

$x \mapsto 3, y \wedge y \mapsto 3, x$

Stack

Heap



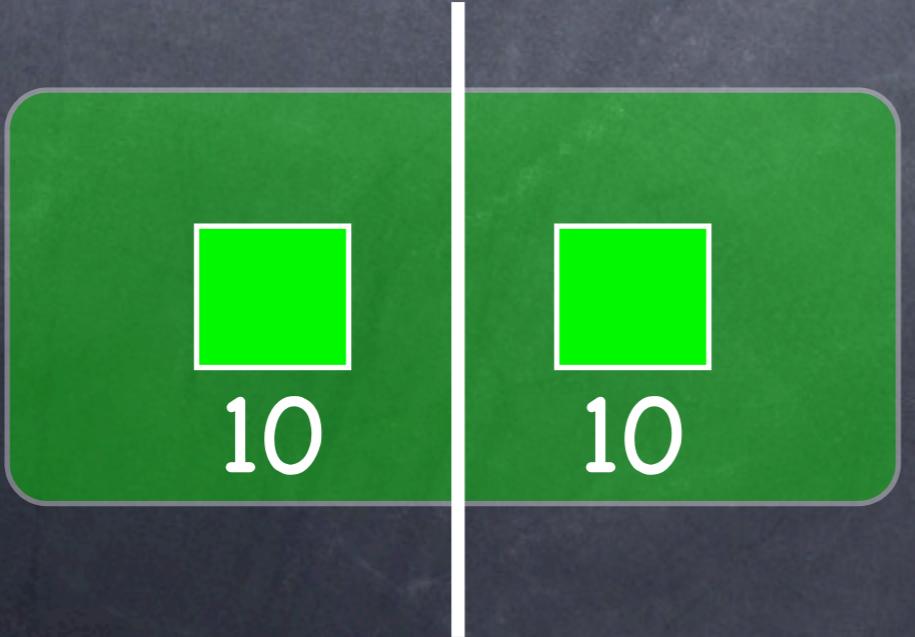
Abbreviation: E points to a record of
several fields: $E \mapsto E_1, \dots, E_n \triangleq E \mapsto E_1 * \dots * E + n - 1 \mapsto E_n$

An inconsistency

- What's wrong with the following formula?
 - $10|^{-}3 * 10|^{-}3$

An inconsistency

- What's wrong with the following formula?
- $10|-\!>3 * 10|-\!>3$



Try to be in two places
at the same time

...back to the real stuff:

Compositional Shape Analysis
by means of Bi-Abduction

Literature

- C. Calcagno, D. Distefano, P. O'Hearn and H. Yang.
Compositional Shape Analysis by Means of Bi-Abduction. POPL 2009.
- D. Distefano. **Attacking Large Industrial Code with Bi-Abductive Inference.** FMICS 2009

A lot of real code out there uses pointer manipulation...

```
void t1394Diag_CancelIrp(PDEVICE_OBJECT DeviceObject, PIRP Irp)
{
    KIRQL           Irql, CancelIrql;
    BUS_RESET_IRP   *BusResetIrp, *temp;
    PDEVICE_EXTENSION deviceExtension;

    deviceExtension = DeviceObject->DeviceExtension;

    KeAcquireSpinLock(&deviceExtension->ResetSpinLock, &Irql);

    temp = (PBUS_RESET_IRP)deviceExtension;
    BusResetIrp = (PBUS_RESET_IRP)deviceExtension->Flink2;

    while (BusResetIrp) {

        if (BusResetIrp->Irp == Irp) {
            temp->Flink2 = BusResetIrp->Flink2;
            free(BusResetIrp);
            break;
        }
        else if (BusResetIrp->Flink2 == (PBUS_RESET_IRP)deviceExtension) {
            break;
        }
        else {
            temp = BusResetIrp;
            BusResetIrp = (PBUS_RESET_IRP)BusResetIrp->Flink2;
        }
    }

    KeReleaseSpinLock(&deviceExtension->ResetSpinLock, Irql);

    IoReleaseCancelSpinLock(Irp->CancelIrql);
    Irp->IoStatus.Status = STATUS_CANCELLED;
    IoCompleteRequest(Irp, IO_NO_INCREMENT);
} // t1394Diag_CancelIrp
```

Is this correct?

Or at least: does it basic properties like it won't crash or leak memory?

We want to build tool that automatically answer such questions

Space Invader analyzer: overview

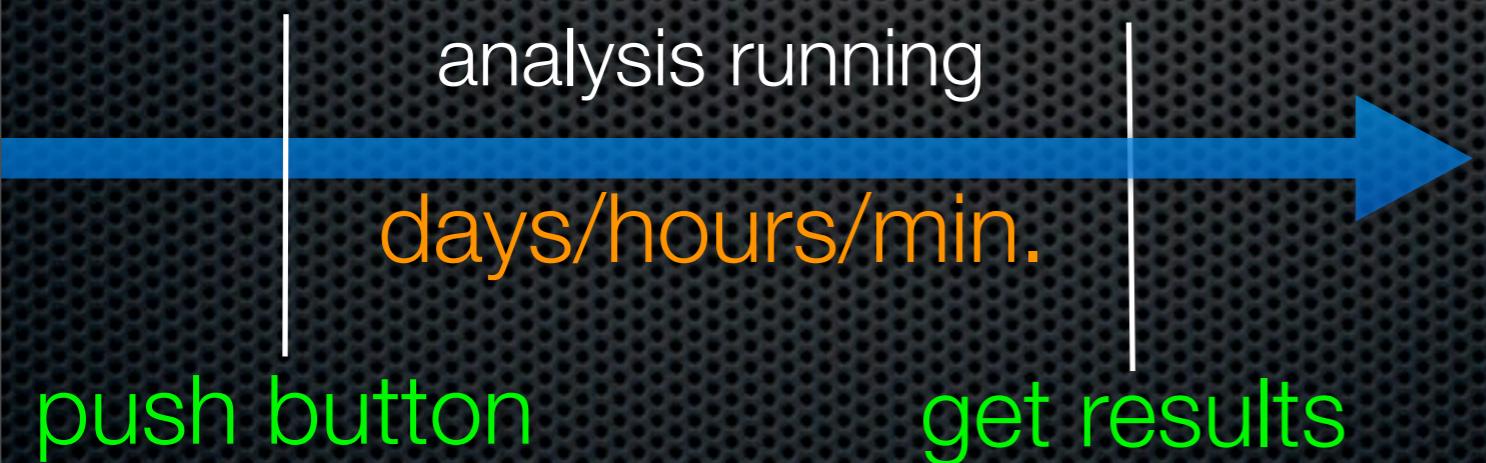
- Shape analyses discover deep properties about the heap: e.g., a variable points to a cyclic/acyclic doubly linked list,...
- Space Invader is Inter-procedural shape analysis for C programs
- Based on Separation Logic and Abstract interpretation to infer invariants
- Builds proofs or reports possible memory faults or memory leaks

Shape Analysis and Real Code

- So far shape analysis mostly applied to toy programs

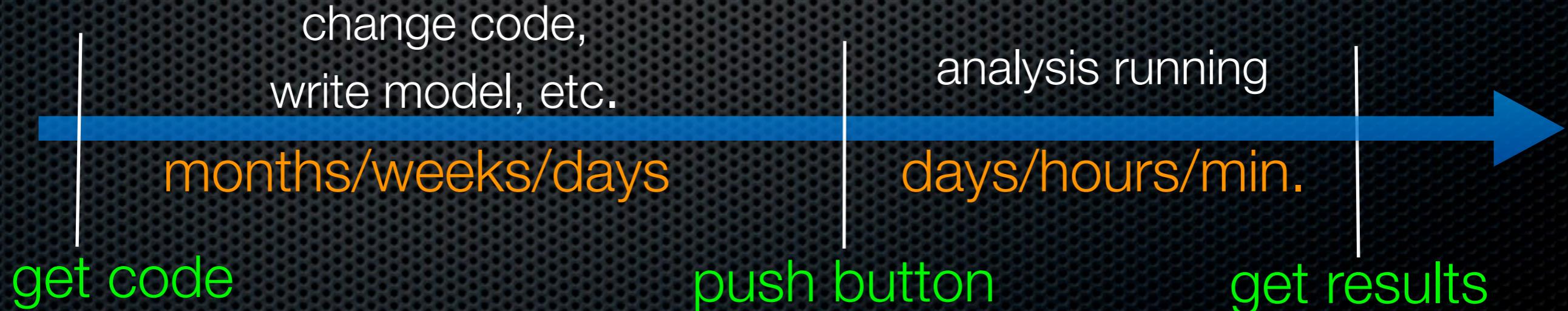
Shape Analysis and Real Code

- So far shape analysis mostly applied to toy programs



Shape Analysis and Real Code

- So far shape analysis mostly applied to toy programs



Fiction:

“no worries, device drivers use mostly lists”

```

typedef struct {
    PDEVICE_OBJECT StackDeviceObject;
    PDEVICE_OBJECT PortDeviceObject;
    PDEVICE_OBJECT PhysicalDeviceObject;

    UNICODE_STRING SymbolicLinkName;
    KSPIN_LOCK ResetSpinLock;
    KSPIN_LOCK CromSpinLock;
    KSPIN_LOCK AsyncSpinLock;
    KSPIN_LOCK IsochSpinLock;
    KSPIN_LOCK IsochResourceSpinLock;

    BOOLEAN bShutdown;
    DEVICE_POWER_STATE CurrentDevicePowerState;
    SYSTEM_POWER_STATE CurrentSystemPowerState;

    ULONG GenerationCount;
} DEVICE_EXTENSION, *PDEVICE_EXTENSION;

```

```

typedef struct ASYNC_ADDRESS_DATA {
    struct ASYNC_ADDRESS_DATA* Flink1;
    struct ASYNC_ADDRESS_DATA* Blink1;
    _PDEVICE_EXTENSION DeviceExtension;
    PVOID Buffer;
    ULONG nLength;
    ULONG nAddressesReturned;
    PADDRESS_RANGE AddressRange;
    HANDLE hAddressRange;
    PMDL pMdl;
} ASYNC_ADDRESS_DATA, *PASYNC_ADDRESS_DATA;

typedef struct BUS_RESET_IRP {
    struct BUS_RESET_IRP *Flink2;
    struct BUS_RESET_IRP *Blink2;
    PIRP Irp;
} BUS_RESET_IRP, *PBUS_RESET_IRP;

typedef struct CROM_DATA {
    struct CROM_DATA *Flink3;
    struct CROM_DATA *Blink3;
    HANDLE hCromData;
    PVOID Buffer;
    PMDL pMdl;
} CROM_DATA, *PCROM_DATA;

typedef struct ISOCH_RESOURCE_DATA {
    struct ISOCH_RESOURCE_DATA *Flink5;
    struct ISOCH_RESOURCE_DATA *Blink5;
    HANDLE hResource;
} ISOCH_RESOURCE_DATA, *PISOCH_RESOURCE_DATA;

```

```

typedef struct {
    PDEVICE_OBJECT
    PDEVICE_OBJECT
    PDEVICE_OBJECT
    PDEVICE_OBJECT

    UNICODE_STRING
    KSPIN_LOCK
    KSPIN_LOCK
    KSPIN_LOCK
    KSPIN_LOCK
    KSPIN_LOCK

    BOOLEAN
    DEVICE_POWER_STATE
    SYSTEM_POWER_STATE

    ULONG
    PASYNC_ADDRESS_DATA
    PASYNC_ADDRESS_DATA
    PBUS_RESET_IRP
    PBUS_RESET_IRP
    PCROM_DATA
    PCROM_DATA
    _PISOCH_DETACH_DATA
    _PISOCH_DETACH_DATA
    PISOCH_RESOURCE_DATA
    PISOCH_RESOURCE_DATA
} DEVICE_EXTENSION, *PDEVICE_EXTENSION;

```

```

typedef struct ASYNC_ADDRESS_DATA {
    struct ASYNC_ADDRESS_DATA* Flink1;
    struct ASYNC_ADDRESS_DATA* Blink1;
    _PDEVICE_EXTENSION DeviceExtension;
    _GUID
    PVOID
    sReturned;
    PADDRESS_RANGE AddressRange;
    HANDLE hAddressRange;
    PMDL pMdl;
} ASYNC_ADDRESS_DATA, *PASYNC_ADDRESS_DATA;

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```

around 600 loc struct definitions

```

typedef struct {
    PDEVICE_OBJECT
    StackDeviceObject;
    PDEVICE_OBJECT
    PortDeviceObject;
    PDEVICE_OBJECT
    PDeviceExtension;
    UNICODE_STRING
    KSPIN_LOCK
    KSPIN_LOCK
    KSPIN_LOCK
    KSPIN_LOCK
    KSPIN_LOCK
    BOOLEAN
    DEVICE_SYSTEM
    ULONG
    PASYNC_ADDRESS_DATA
    PASYNC_ADDRESS_DATA
    PBUS_RESET_IRP
    PBUS_RESET_IRP
    PCROM_DATA
    PCROM_DATA
    _PISOCH_DETACH_DATA
    _PISOCH_DETACH_DATA
    PISOCH_RESOURCE_DATA
    PISOCH_RESOURCE_DATA
} DEVICE_EXTENSION, *PDEVICE_EXTENSION;

```

```

typedef struct ASYNC_ADDRESS_DATA {
    struct ASYNC_ADDRESS_DATA* Flink1;
    struct ASYNC_ADDRESS_DATA* Blink1;
    _PDEVICE_EXTENSION DeviceExtension;
    _GUID
    Puff
    sReturned;
}

```

around 600 loc struct definitions

```

PADDRESS_RANGE AddressRange;
HANDLE hAddressRange;
PMDL pMdl;
} ASYNC_ADDRESS_DATA, *PASYNC_ADDRESS_DATA;

```

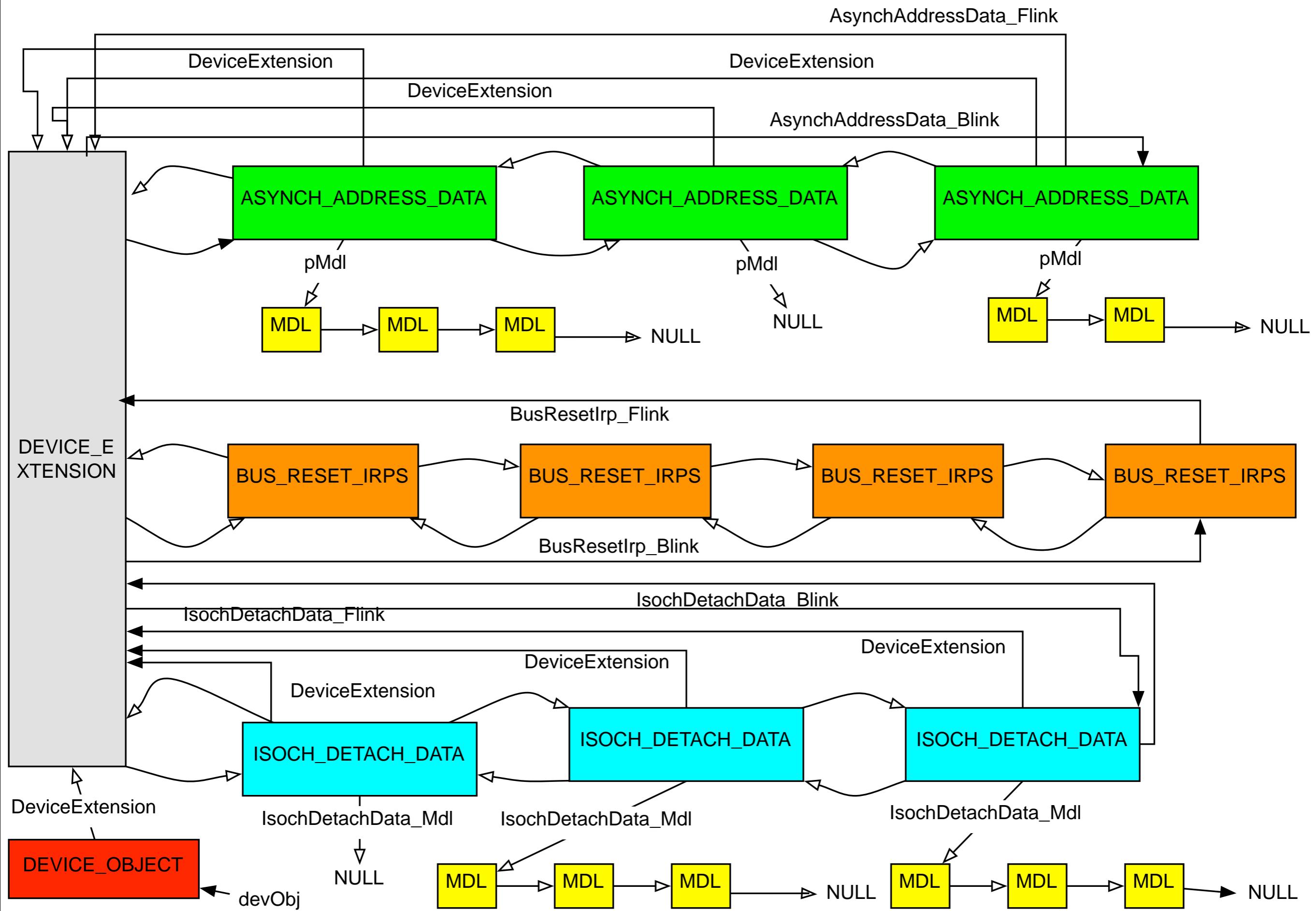
many big structs (around 20 fields) mutually pointing to each other in several way with several fields

```

    struct CROM_DATA *Blink3;
    HANDLE hCromData;
    PVOID Buffer;
    PMDL pMdl;
} CROM_DATA, *PCROM_DATA;

typedef struct ISOCH_RESOURCE_DATA {
    struct ISOCH_RESOURCE_DATA *Flink5;
    struct ISOCH_RESOURCE_DATA *Blink5;
    HANDLE hResource;
} ISOCH_RESOURCE_DATA, *PISOCH_RESOURCE_DATA;

```



Fact:

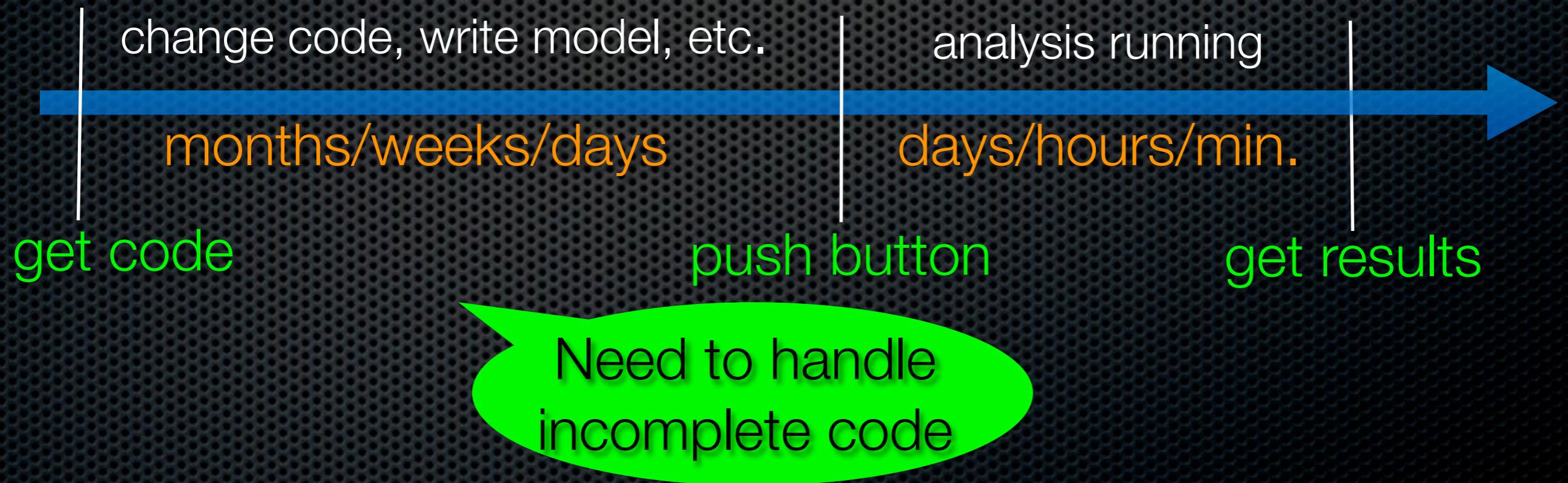
Real device drivers use lists in combination, resulting in more complicated data structures than those found in previous papers on shape analysis

Shape Analysis and Real Code

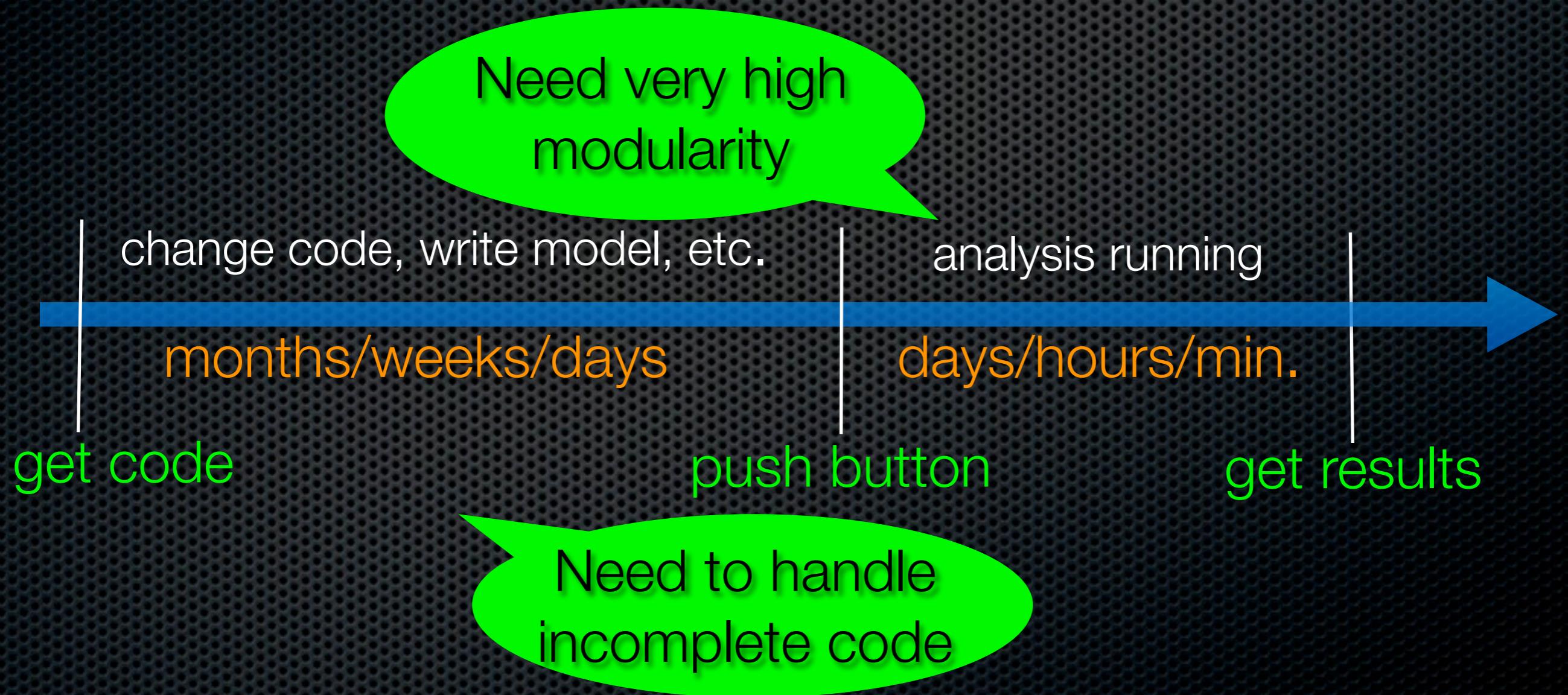
Shape Analysis and Real Code



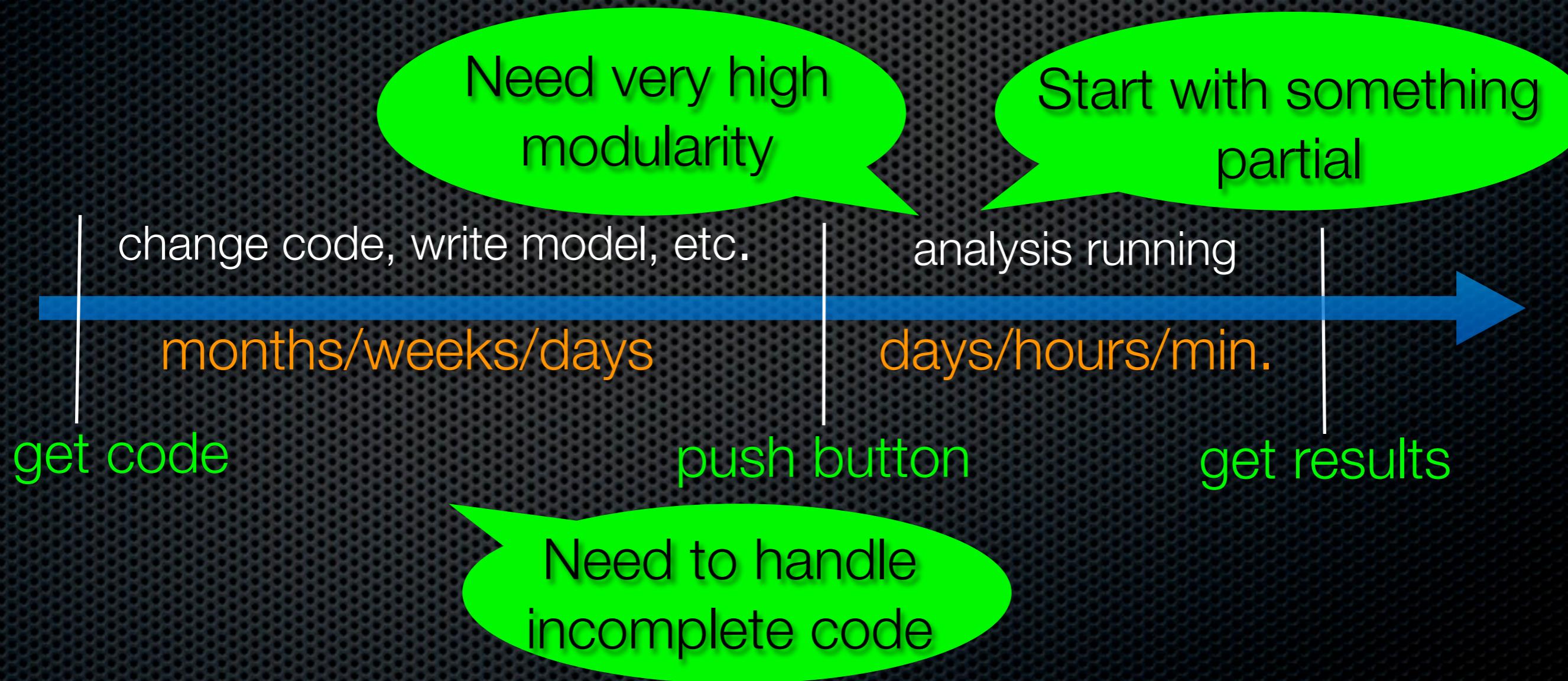
Shape Analysis and Real Code



Shape Analysis and Real Code



Shape Analysis and Real Code



Our response: compositional Space Invader

- ✓ Handles incomplete code
- ✓ Admits partial results
- ✓ Modular

Our response: compositional Space Invader

- ✓ Handles incomplete code
- ✓ Admits partial results
- ✓ Modular

...demo!

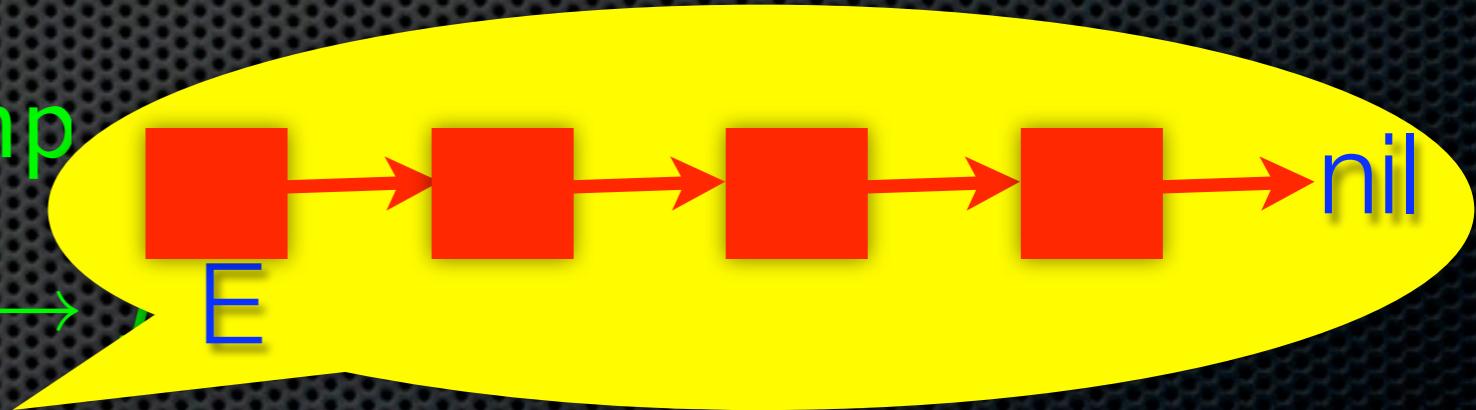
Basics

Notation

- Separation Logic's formulae to represent program states
- Some useful predicates:
 - The empty heap: emp
 - An allocated cell: $E \mapsto F$
 - A “complete” list: $\text{list}(E)$
- P^*Q means P and Q hold for **disjoint** portion of memory

Notation

- Separation Logic's formulae to represent program states
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 - An allocated cell: $E \mapsto$
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Notation

- Separation Logic's formulae to represent program states
- Some useful predicates:
 - The empty heap: emp
 - An allocated cell: $E \mapsto F$
 - A “complete” list: $\text{list}(E)$
- P^*Q means P and Q hold for **disjoint** portion of memory

Small specs

- Small specs encourage local reasoning and help to get small proofs
- When proving code involving procedures we use only their **footprint**

Example: use of small specs in proofs

{list(l1)*list(l2)}

Dispose(l1);

Dispose(l2);

Spec: {list(l)} Dispose(l) {emp}

$$\frac{\{P\} C \{Q\}}{\{P^*R\} C \{Q^*R\}} \text{ Frame Rule}$$

Example: use of small specs in proofs

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{list(l1)*list(l2)}

Dispose(l1);

{emp*list(l2)}

Dispose(l2);

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$$\frac{\{P\} \subset \{Q\}}{\{P^*R\} \subset \{Q^*R\}} \text{ Frame Rule}$$

Example: use of small specs in proofs

{list(l1)*list(l2)}

Dispose(l1);

{list(l2)}

Dispose(l2);

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Example: use of small specs in proofs

{list(l1)*list(l2)}

Dispose(l1);

{list(l2)}

Dispose(l2);

{emp}

Spec: {list(l)} Dispose(l) {emp}

$$\frac{\{P\} \subset \{Q\}}{\{P^*R\} \subset \{Q^*R\}} \text{ Frame Rule}$$

Novelties

Frame Inference

```
{list(l1)*list(l2)}  
Dispose(l1);  
  
Dispose(l2);
```

$$\frac{\{P\} \subset \{Q\}}{\{P^*R\} \subset \{Q^*R\}} \text{ Frame Rule}$$

Spec: {list(1)} Dispose(1) {emp}

Frame Inference

```
{list(l1)*list(l2)}  
Dispose(l1);
```

```
Dispose(l2);
```

$$\frac{\{P\} \subset \{Q\}}{\{P^*R\} \subset \{Q^*R\}} \quad \text{Frame Rule}$$

Spec: {list(1)} Dispose(1) {emp}

- In analysis to use the Frame Rule we need to compute R
- Frame inference problem: given A and B compute X such that $A \vdash B*X$

Frame Inference

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{list(l1)*list(l2)}  
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Example:

```
list(l1)*list(l2) ⊢ list(l1)* X
```

Frame Inference

```
{list(l1)*list(l2)}  
Dispose(l1);
```

```
Dispose(l2);
```

$$\frac{\{P\} \subset \{Q\}}{\{P^*R\} \subset \{Q^*R\}} \text{ Frame Rule}$$

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Example:

```
list(l1)*list(l2) ⊢ list(l1)*list(l2)
```

Frame Inference

```
{list(l1)*list(l2)}  
Dispose(l1);
```

$$\frac{\{P\} \subset \{Q\}}{\{P^*R\} \subset \{Q^*R\}} \quad \text{Frame Rule}$$

```
Dispose(l2);
```

Spec: {list(1)} Dispose(1) {emp}

- In analysis to use the Frame Rule we need to compute R
- Frame inference problem: given A and B compute X such that $A \vdash B*X$

Example:

```
list(l1)*list(l2) ⊢ list(l1)*list(l2)
```

Frame Inference

```
{list(l1)*list(l2)}  
Dispose(l1);  
{emp*list(l2)}  
Dispose(l2);
```

$$\frac{\{P\} \subset \{Q\}}{\{P^*R\} \subset \{Q^*R\}} \quad \text{Frame Rule}$$

Spec: {list(1)} Dispose(1) {emp}

- In analysis to use the Frame Rule we need to compute R
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Example:

```
list(l1)*list(l2) ⊢ list(l1)*list(l2)
```

Abduction

Abductive Inference

(Charles Peirce, circa 1900, writing about the scientific process)



"Abduction is the process of forming an explanatory hypothesis. It is the only logical operation which introduces any new idea"

"A man must be downright crazy to deny that science has made many true discoveries. But every single item of scientific theory which stands established today has been due to Abduction."

The Collected Papers of Charles Sanders Peirce, Volume V,
Pragmatism and Pragmaticism

Abduction for Space Invader

Abduction for Space Invader



Abduction for Space Invader

Abduction Inference:

given A and B compute X such that

$$A * X \vdash B$$



Abduction for Space Invader

Abduction Inference:

given A and B compute X such that

$$A*X \vdash B$$



Example:

Spec: {list(l1)*list(l2)} Dispose_Two_Lists(l1,l2) {emp}

list(l1)

Abduction for Space Invader

Abduction Inference:

given A and B compute X such that

$$A * X \vdash B$$



Example:

Spec: {list(l1)*list(l2)} Dispose_Two_Lists(l1,l2) {emp}

$$\text{list}(l1)*x \vdash \text{list}(l1)*\text{list}(l2)$$

Abduction for Space Invader

Abduction Inference:

given A and B compute X such that

$$A * X \vdash B$$



Example:

Spec: {list(l1)*list(l2)} Dispose_Two_Lists(l1,l2) {emp}

$$\text{list(l1)*list(l2)} \vdash \text{list(l1)*list(l2)}$$

Abduction is not enough

If heaps A and B are incomparable abduction and frame inference alone are not enough.

We need to synthesize both missing portion of state and leftover portion of state

Heap A

$$x \mapsto y * y \mapsto y'$$

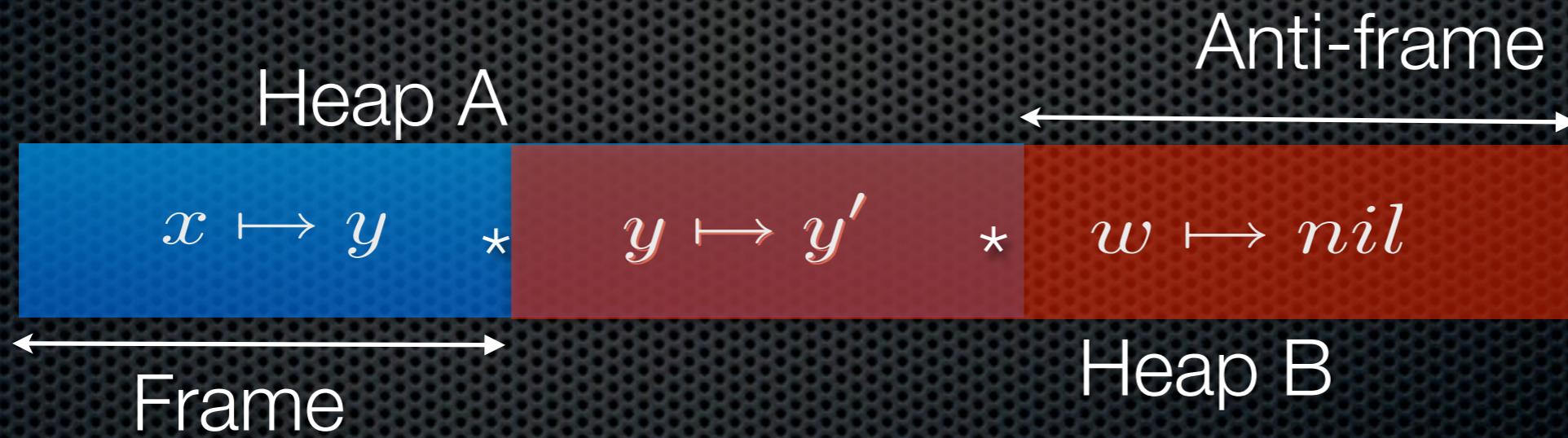
$$y \mapsto y' * w \mapsto nil$$

Heap B

Abduction is not enough

If heaps A and B are incomparable abduction and frame inference alone are not enough.

We need to synthesize both missing portion of state and leftover portion of state



Bi-Abduction

Synthesizing both missing portion of state (**anti-frame**) and leftover portion of state (**frame**) give rise to a new notion

Bi-Abduction:

given A and B compute **?antiframe** and **?frame** such that

$$A * \text{?antiframe} \vdash B * \text{?frame}$$

Bi-Abduction

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Bi-Abduction:

given A and B compute **?antiframe** and **?frame** such that

$$A * \text{?antiframe} \vdash B * \text{?frame}$$

Example:

$$x \mapsto 0 * z \mapsto 0 * \text{?antiframe} \vdash \text{list}(x) * \text{list}(y) * \text{?frame}$$

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Our POPL'09 paper defines a theorem prover for Bi-Abduction

Bi-Abductive spec synthesis

Pre: `list(x) * list(y)`

`void foo(list_item *x,list_item *y)`

Post: `list(x)`

```
1 void p(list_item *y) { emp  
2     list_item *x, *z;  
3     x=malloc(sizeof(list_item)); x->tail = 0; emp  
4     z=malloc(sizeof(list_item)); z->tail = 0;  
5     foo(x,y);  
6     foo(x,z);  
7 }
```



Bi-abductive prover

Bi-Abductive spec synthesis

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7 }
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Bi-abductive prover

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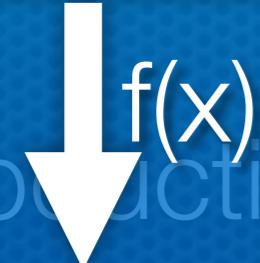
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5     foo(x,y); x ↦ 0 * z ↦ 0  
6     foo(x,z);
```



7 ↦ 1

H



Bi-abductive prover

Pre

f(x)

Post

FootPrint

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

```
1 void p(list_item *y) { emp  
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5     foo(x,y); x ↦ 0 * z ↦ 0  
6     foo(x,z);
```



7 ↳

H

Pre

f(x)

Post

Bi-abductive prover

FootPrint

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

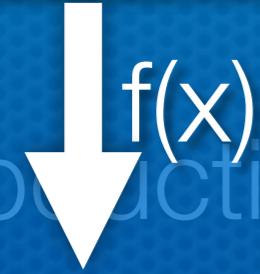
```
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4     z=malloc(sizeof(list_item)); z->tail = 0; x ↦ 0  
5     foo(x,y); x ↦ 0 * z ↦ 0  
6     foo(x,z);
```



7 ↴

Frame

Pre



Bi-abductive prover

f(x) Post

FootPrint

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

```
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4   z=malloc(sizeof(list_item)); z->tail = 0; x ↦ 0  
5   foo(x,y); x ↦ 0 * z ↦ 0  
6   foo(x,z);
```



7 ↲

Frame

AntiF

f(x) Post



Bi-abductive prover

FootPrint

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

```
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5   foo(x,y); x ↦ 0 * z ↦ 0  
6   foo(x,z);
```



7 ↳

H

AntiF

f(x) Post



Bi-abductive prover

Frame

FootPrint

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Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

```
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```



7 ↳

H

AntiF

f(x)

f(x)

Bi-abductive prover

Frame

Post

FootPrint

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

```
1 void p(list_item *y) { emp  
2     list_item *x, *z;  
3     x=malloc(sizeof(list_item)); x->tail = 0; emp  
4     z=malloc(sizeof(list_item)); z->tail = 0; x ↦ 0  
5     foo(x,y);  
6     foo(x,z);  
7 }
```

→ $x \mapsto 0 * z \mapsto 0$

H

Pre

f(x)



Bi-abductive prover

Frame

Post

AntiF FootPrint

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Bi-abductive prover

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```



Bi-abductive prover

$$x \mapsto 0 * z \mapsto 0 * ?antiframe \vdash \text{list}(x) * \text{list}(y) * ?frame$$

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7 }
```



Bi-abductive prover

$$x \mapsto 0 * z \mapsto 0 * \text{list}(y) \vdash \text{list}(x) * \text{list}(y) * z \mapsto 0$$

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x,list_item *y)

Post: $\text{list}(x)$

```
1 void p(list_item *y) { list(y)
2   list_item *x, *z;
3   x=malloc(sizeof(list_item)); x->tail = 0; emp
4   z=malloc(sizeof(list_item)); z->tail = 0; x ↦ 0
5   foo(x,y);
6   foo(x,z); x ↦ 0 * z ↦ 0
7 }
```

list(x) * $z \mapsto 0$

Bi-abductive prover

$$x \mapsto 0 * z \mapsto 0 * \text{list}(y) \vdash \text{list}(x) * \text{list}(y) * z \mapsto 0$$

Bi-Abductive spec synthesis

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```

list(x) * $z \mapsto 0$

Bi-abductive prover

$$\text{list}(x) * z \mapsto 0 * ?\text{antiframe} \vdash \text{list}(x) * \text{list}(z) * ?\text{frame}$$

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

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7 }
```

list(x) * $z \mapsto 0$

Bi-abductive prover

$\text{list}(x) * z \mapsto 0 * \text{emp} \vdash \text{list}(x) * \text{list}(z) * \text{emp}$

Bi-Abductive spec synthesis

Pre: $\text{list}(x) * \text{list}(y)$

void foo(list_item *x, list_item *y)

Post: $\text{list}(x)$

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5   foo(x,y);
6   foo(x,z); x ↦ 0 * z ↦ 0
7 }
```

list(x) * $z \mapsto 0$
list(x)



Bi-abductive prover

$$\text{list}(x) * z \mapsto 0 * \text{emp} \vdash \text{list}(x) * \text{list}(z) * \text{emp}$$

General Schema Compositional Analysis

For function in the program we compute tables of specs

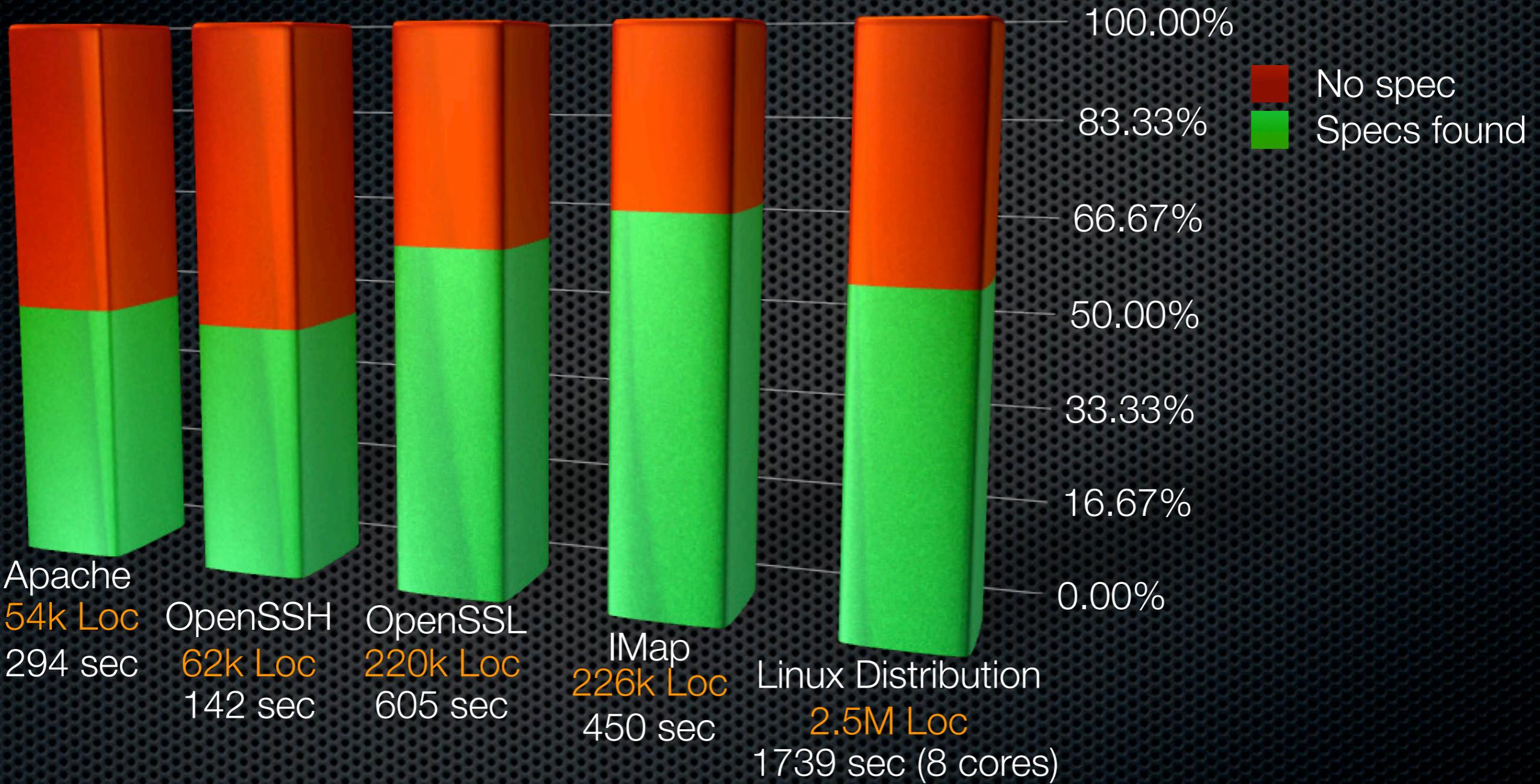
$$\{T_{f_1}, \dots, T_{f_n}\}$$

Tables are sets of entries of type: $(pre, \{post_1, post_2, \dots\})$

The computation follows the call graph (start from leaves)

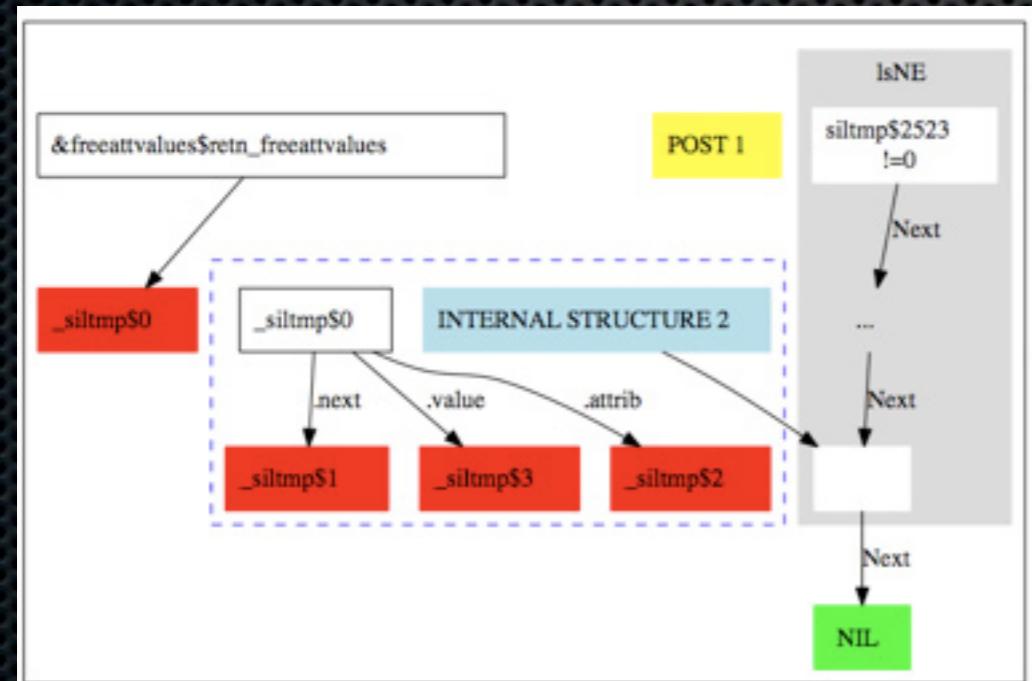
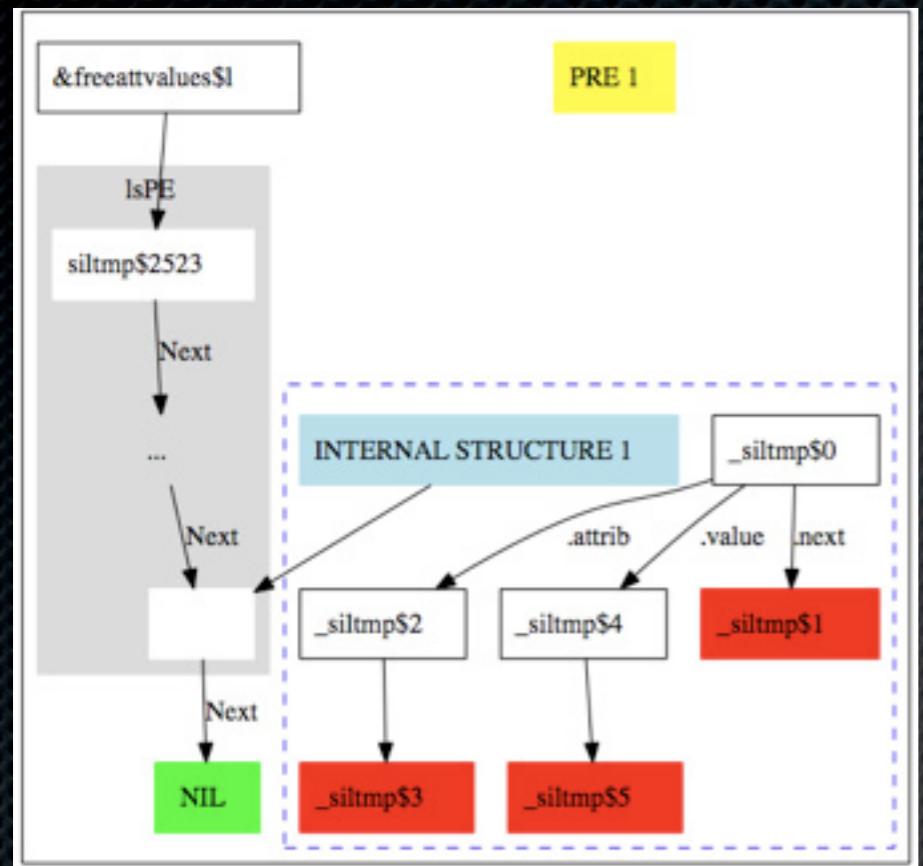
Recursive functions are analyzed with an iterative method until it reaches fixed point

Running on really big code

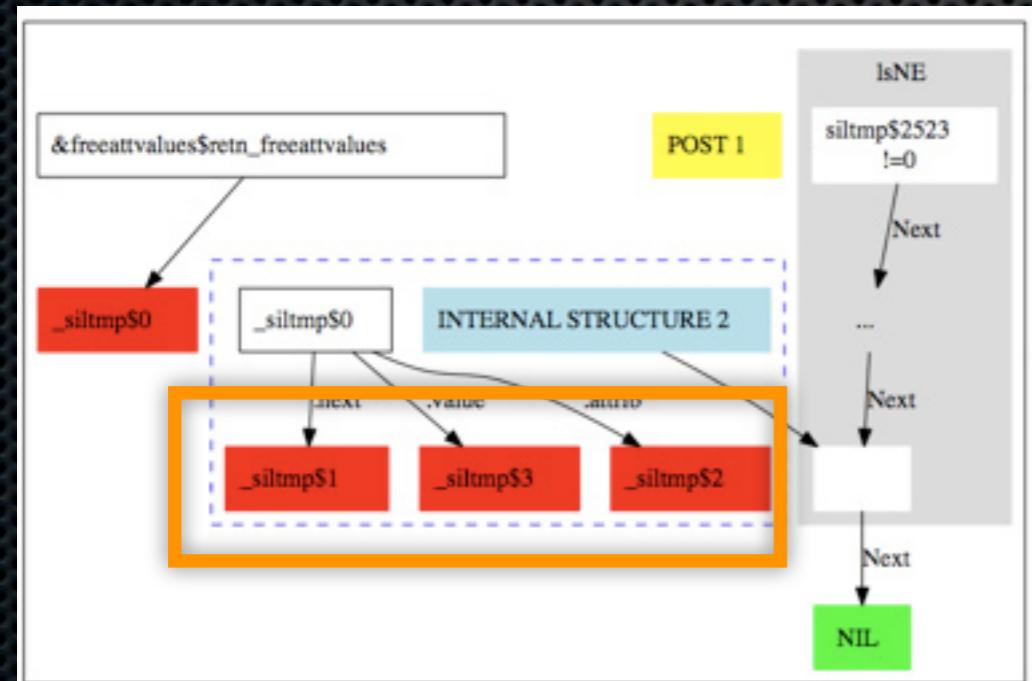
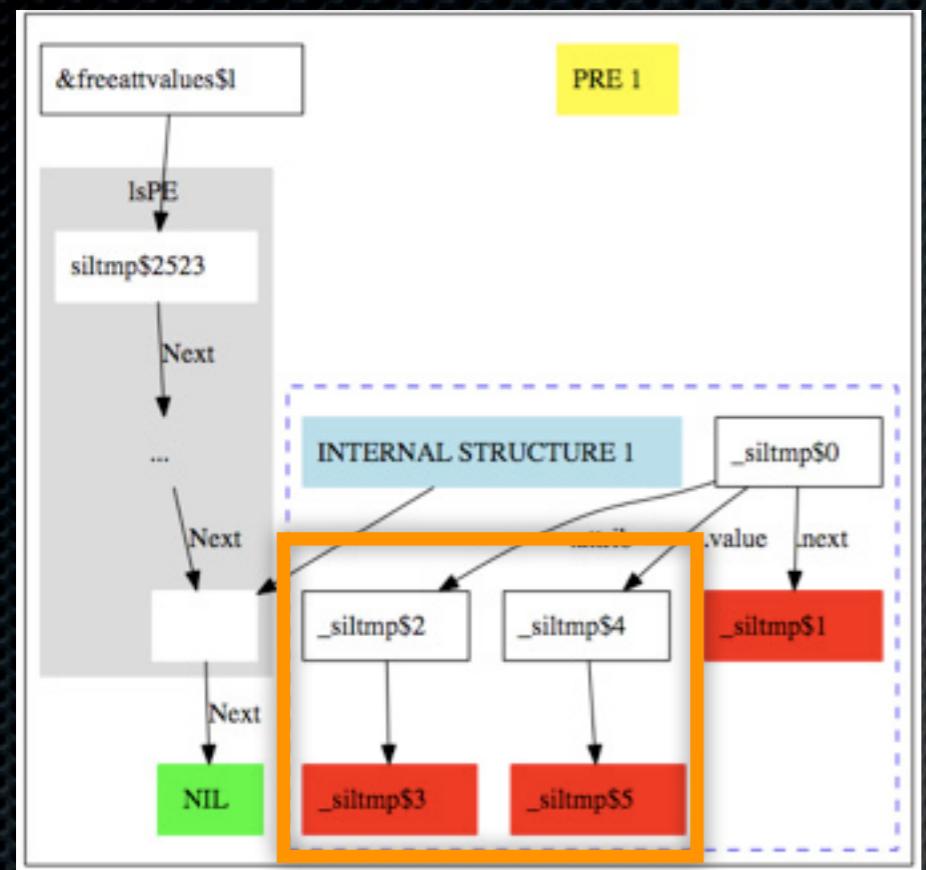


Test for precision: run on Firewire device driver and small recursive procedures handling nested data structures

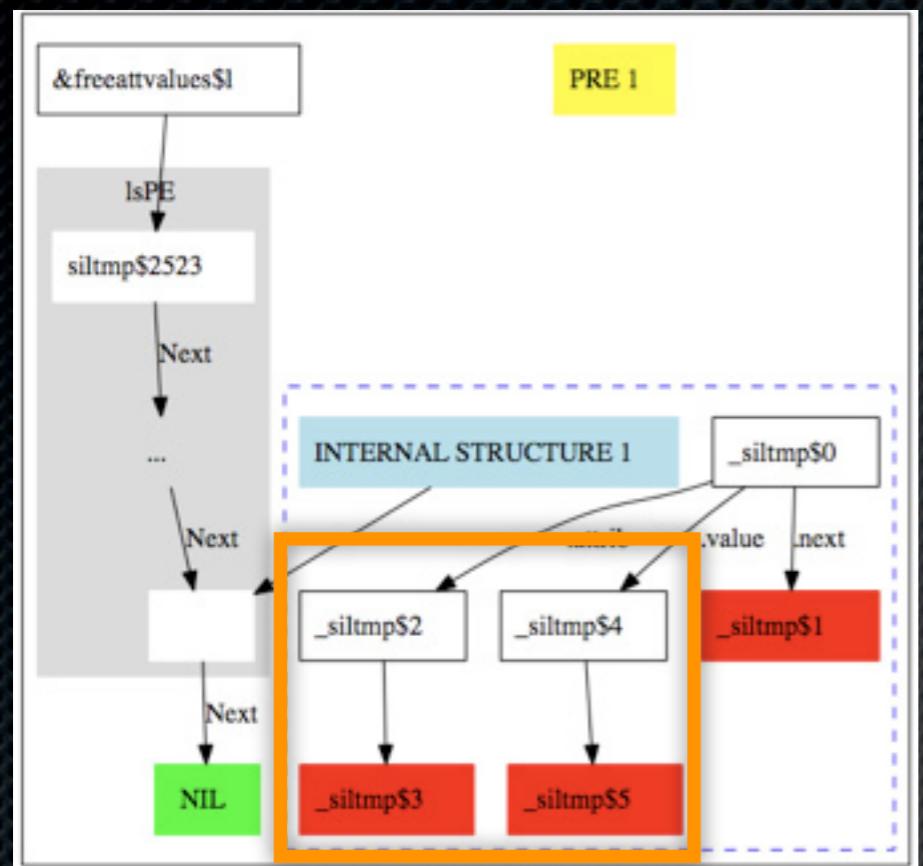
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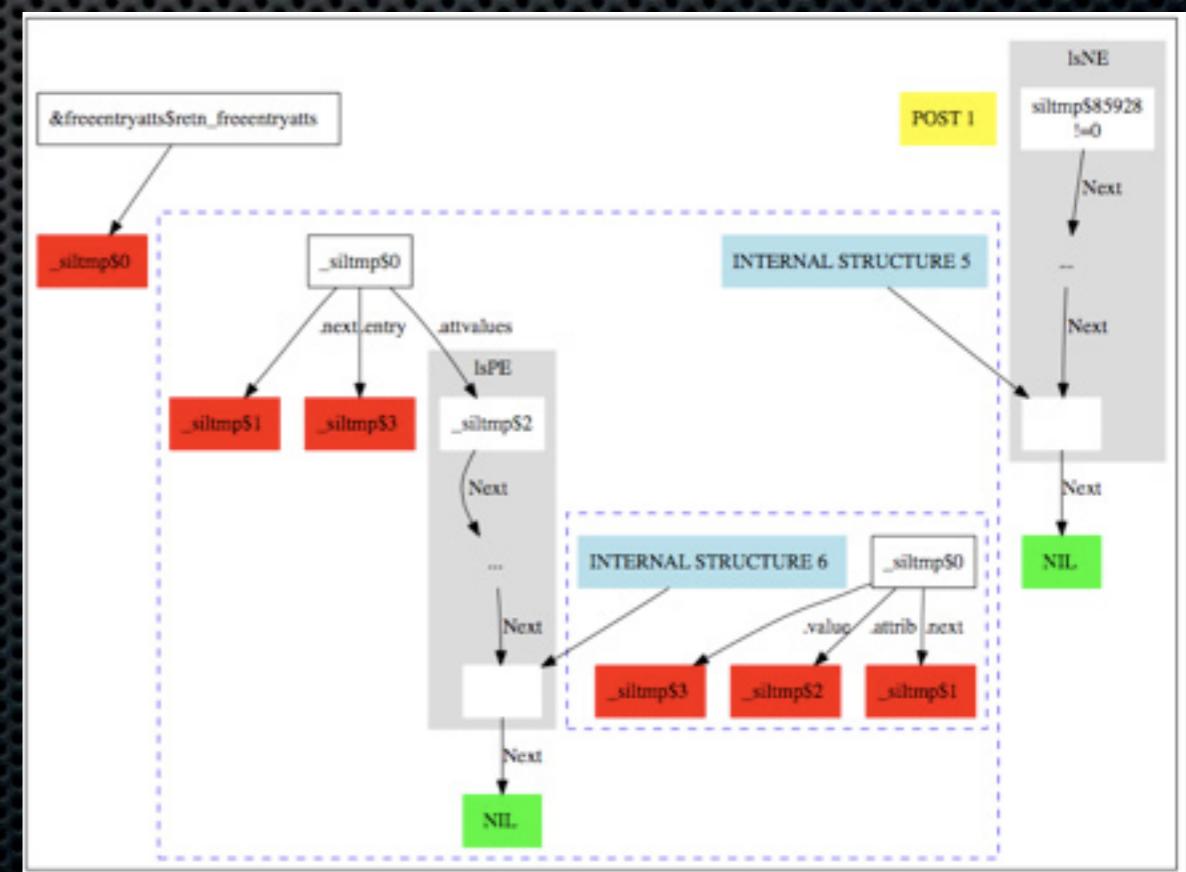
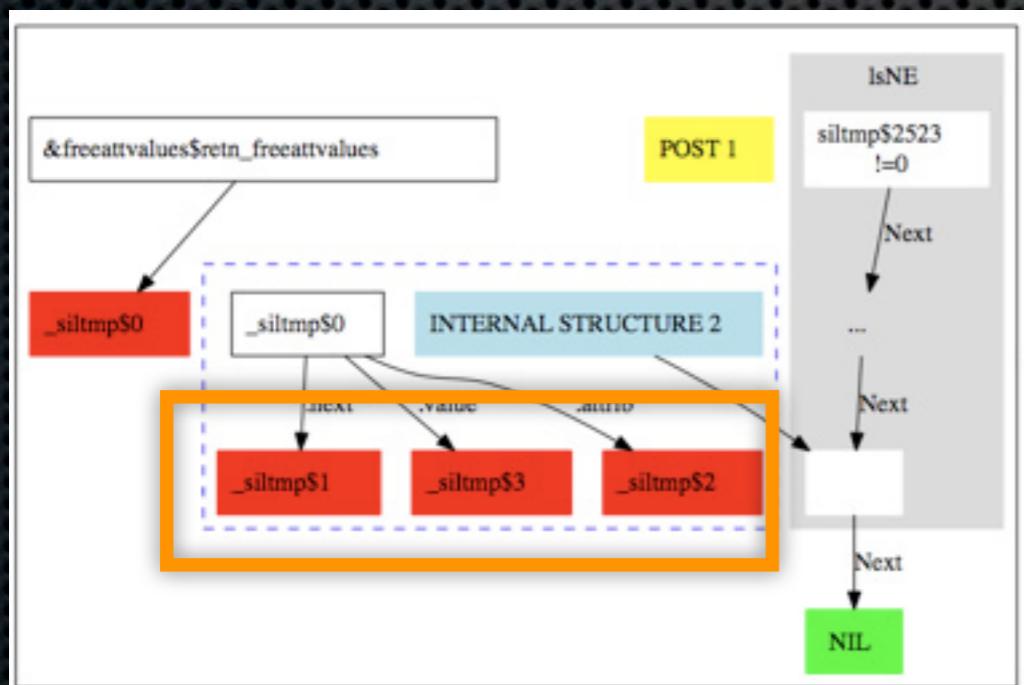
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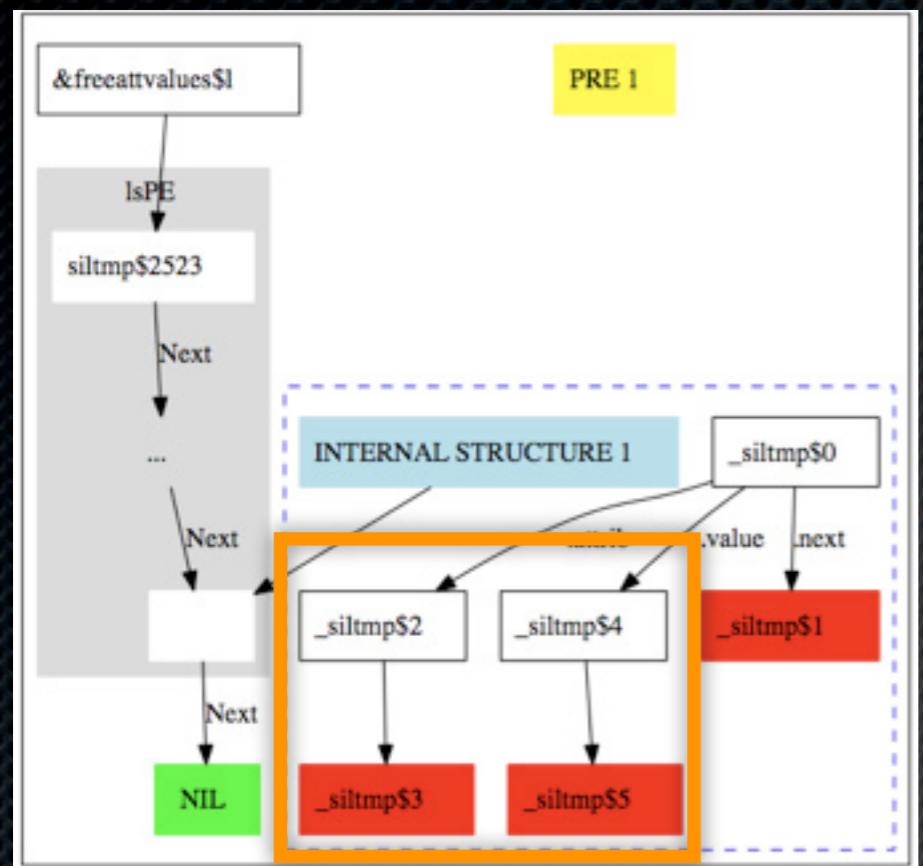
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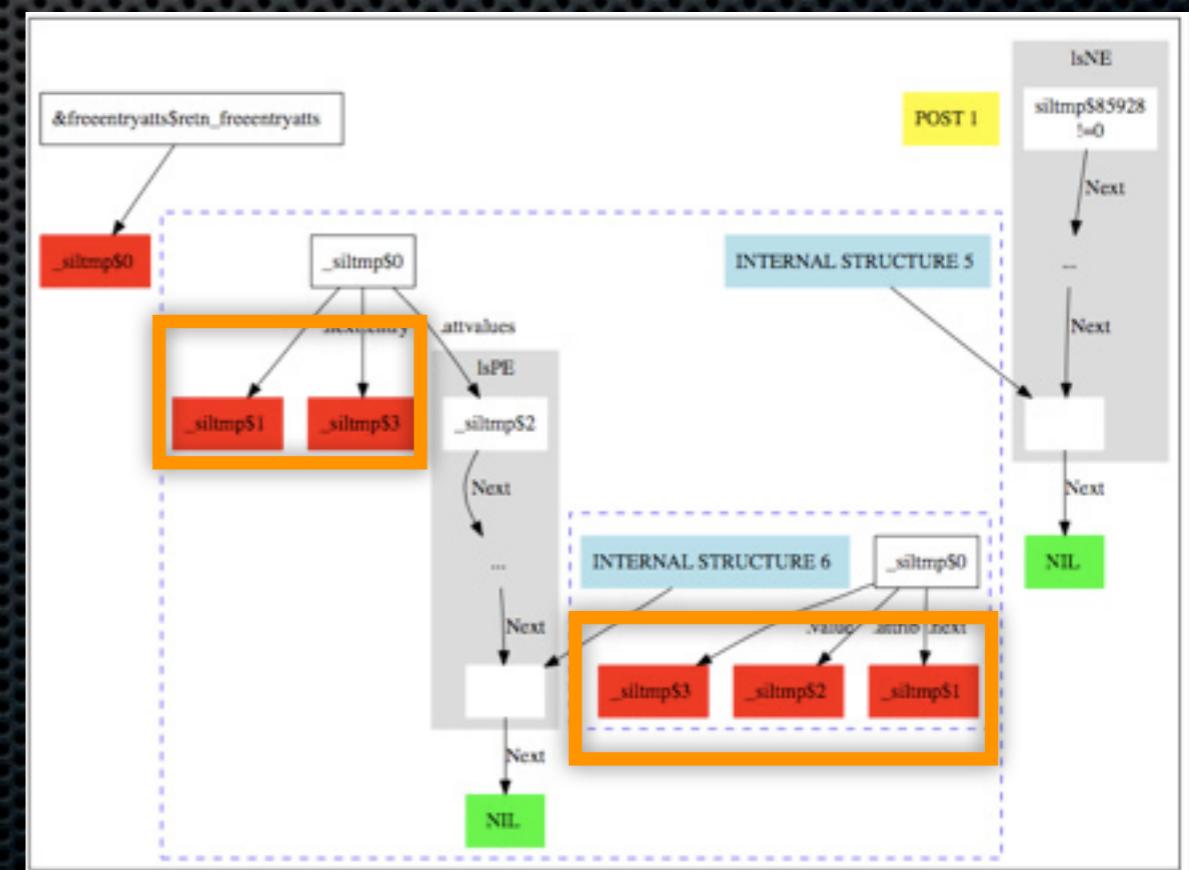
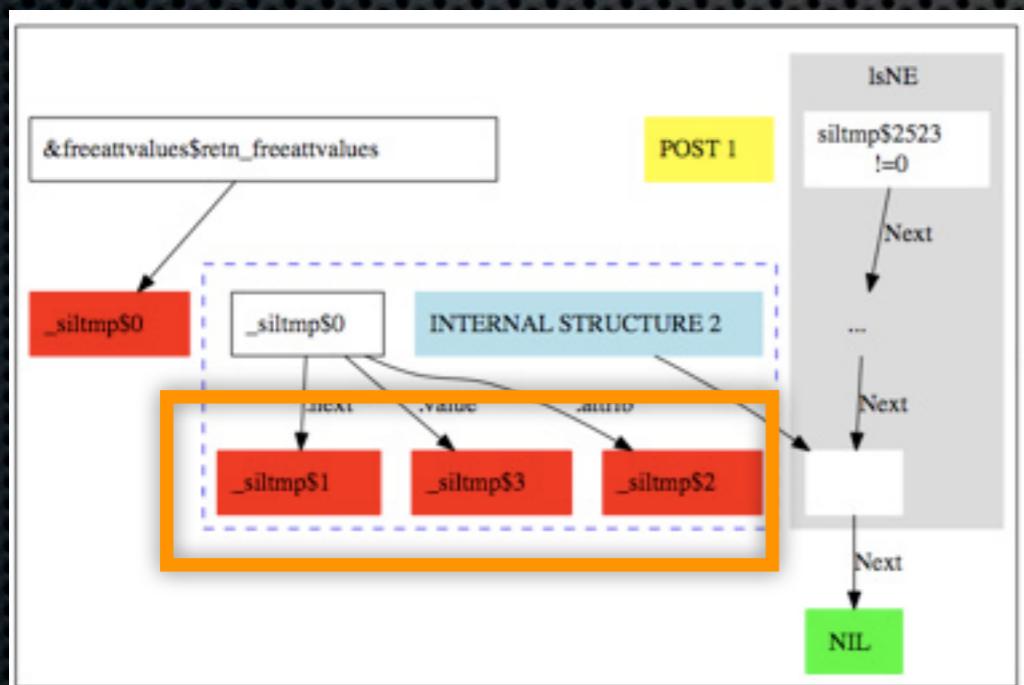
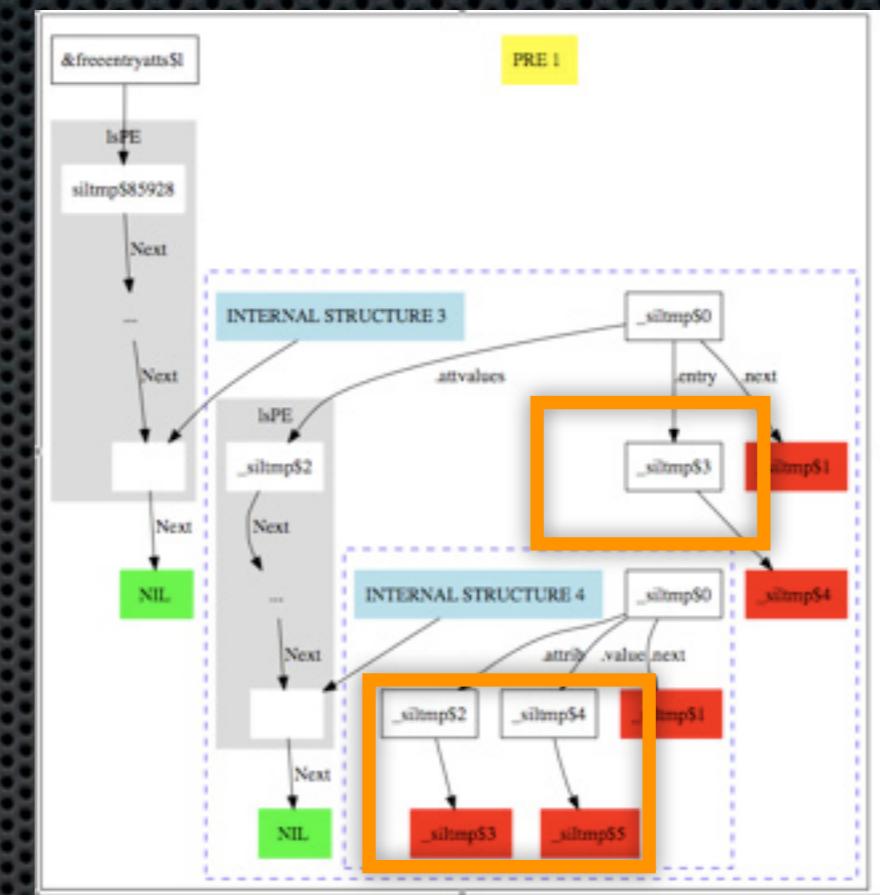
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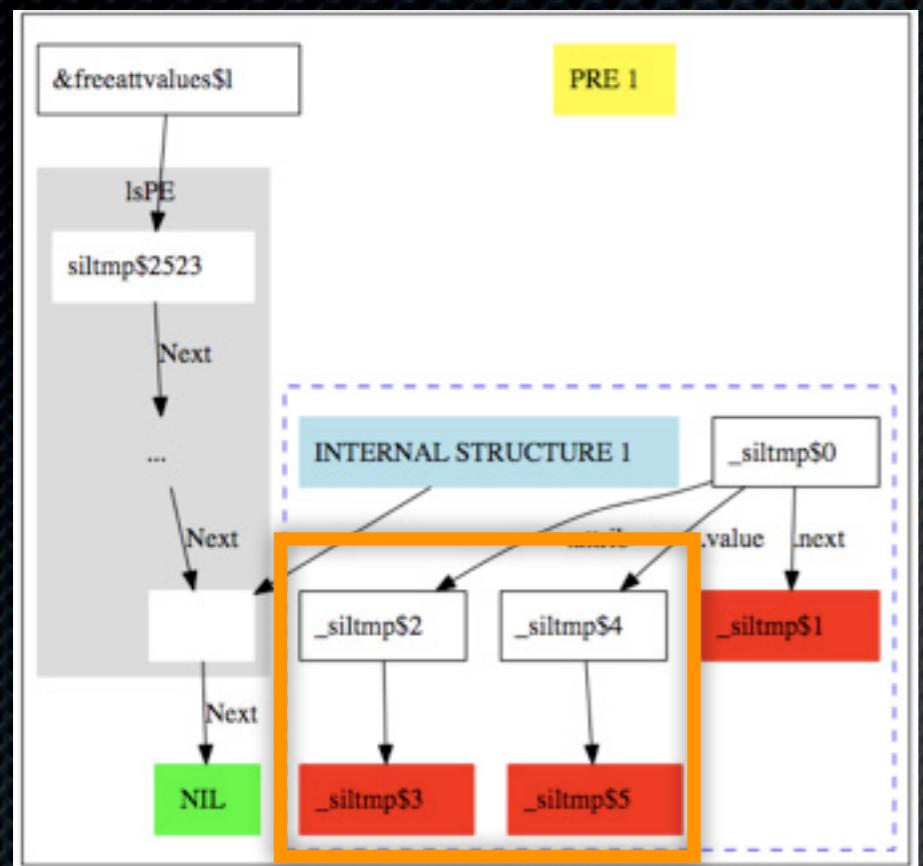
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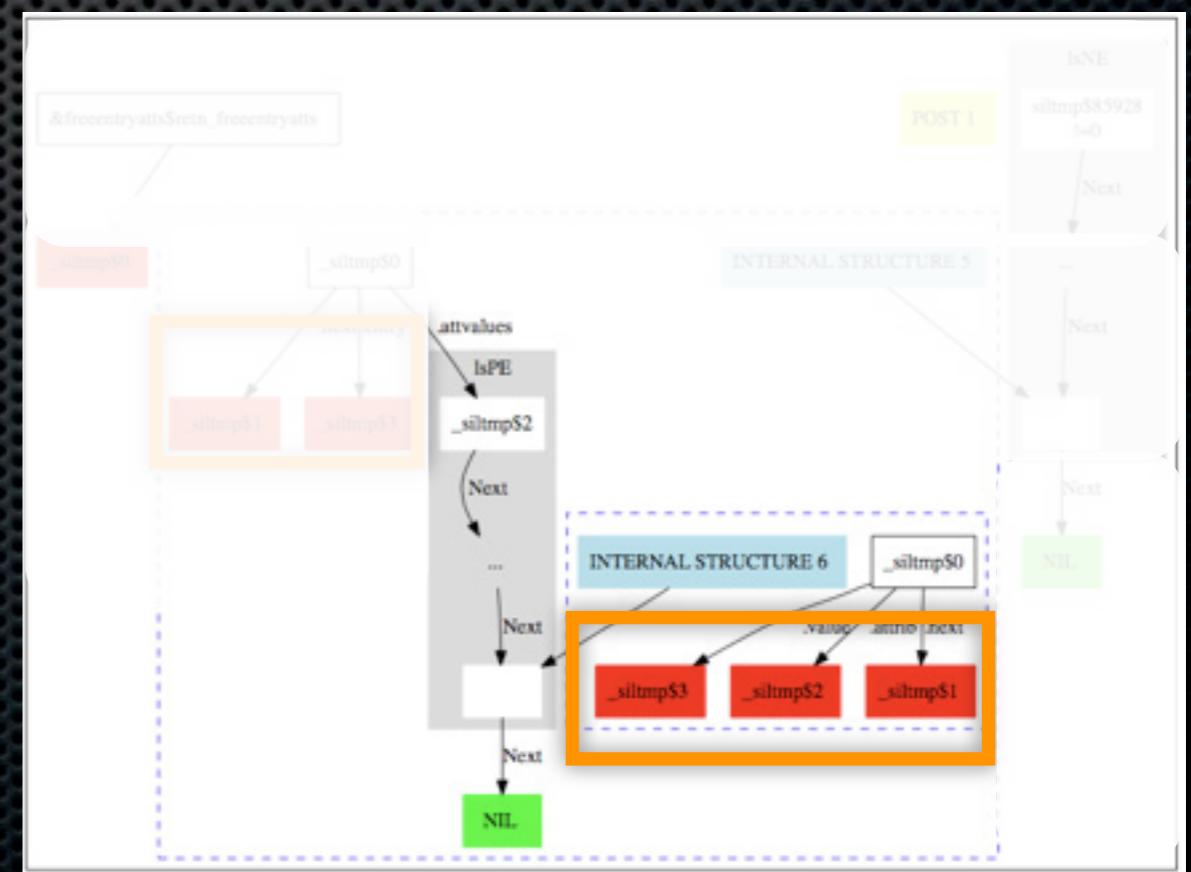
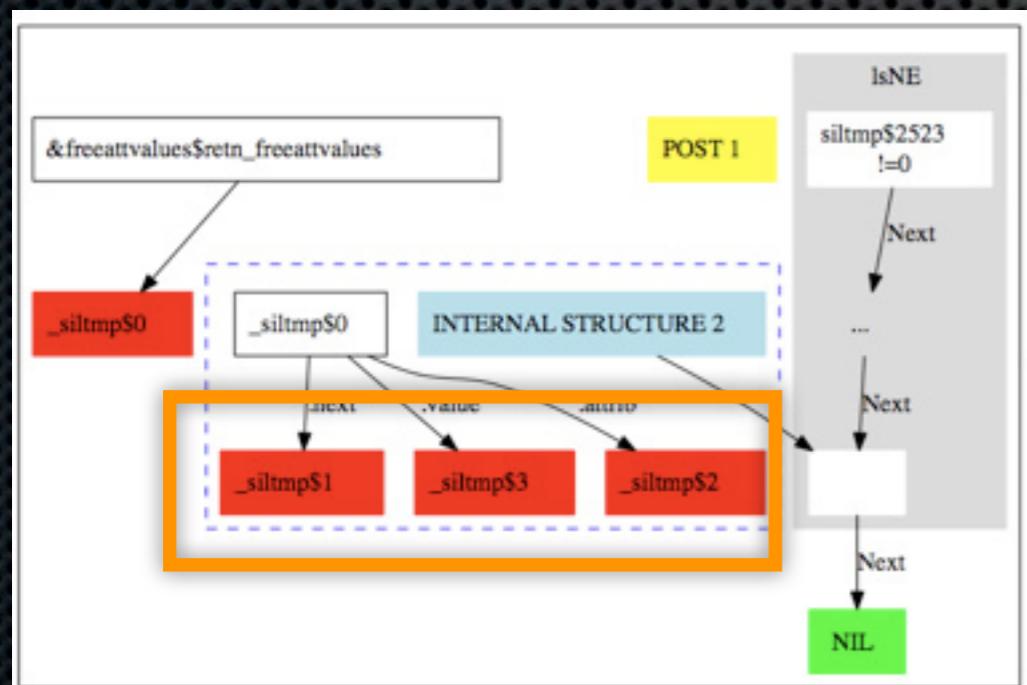
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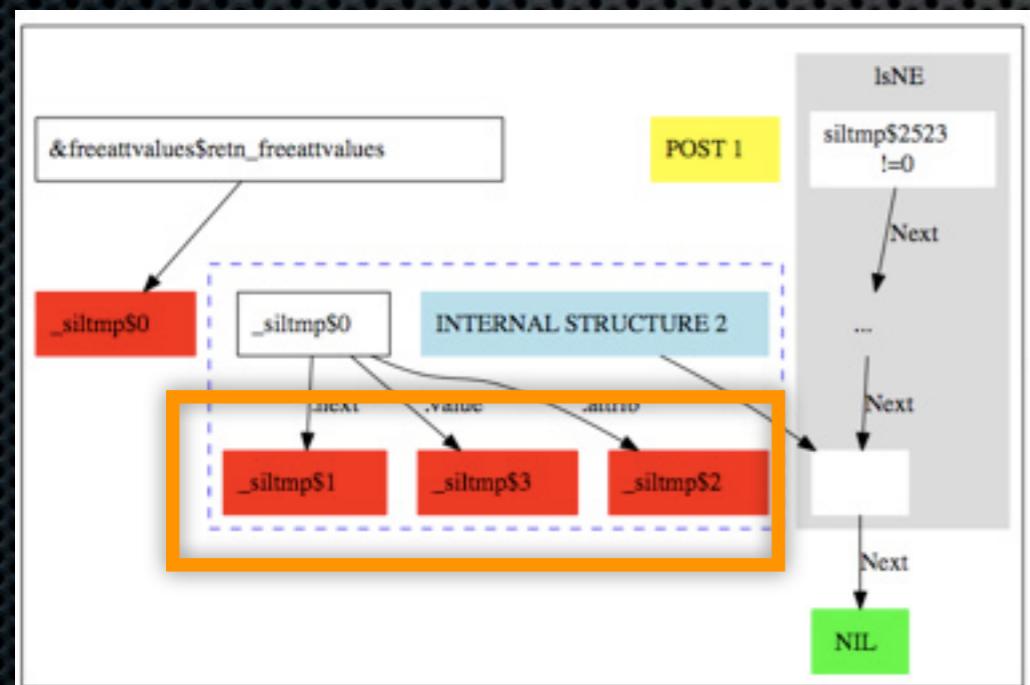
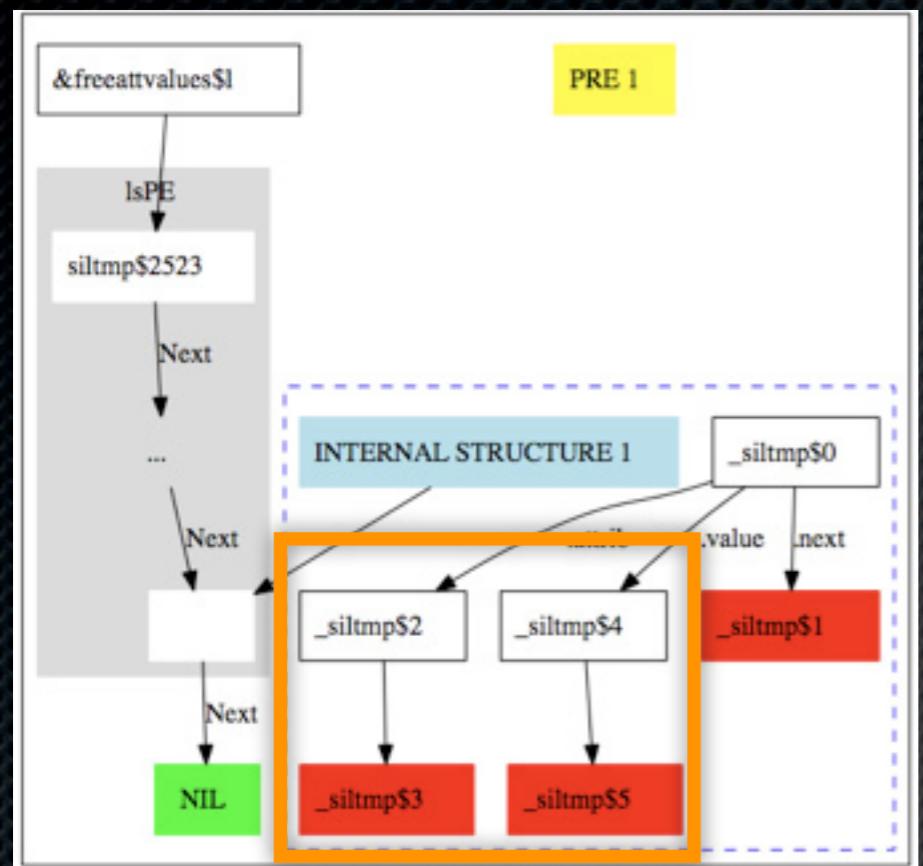
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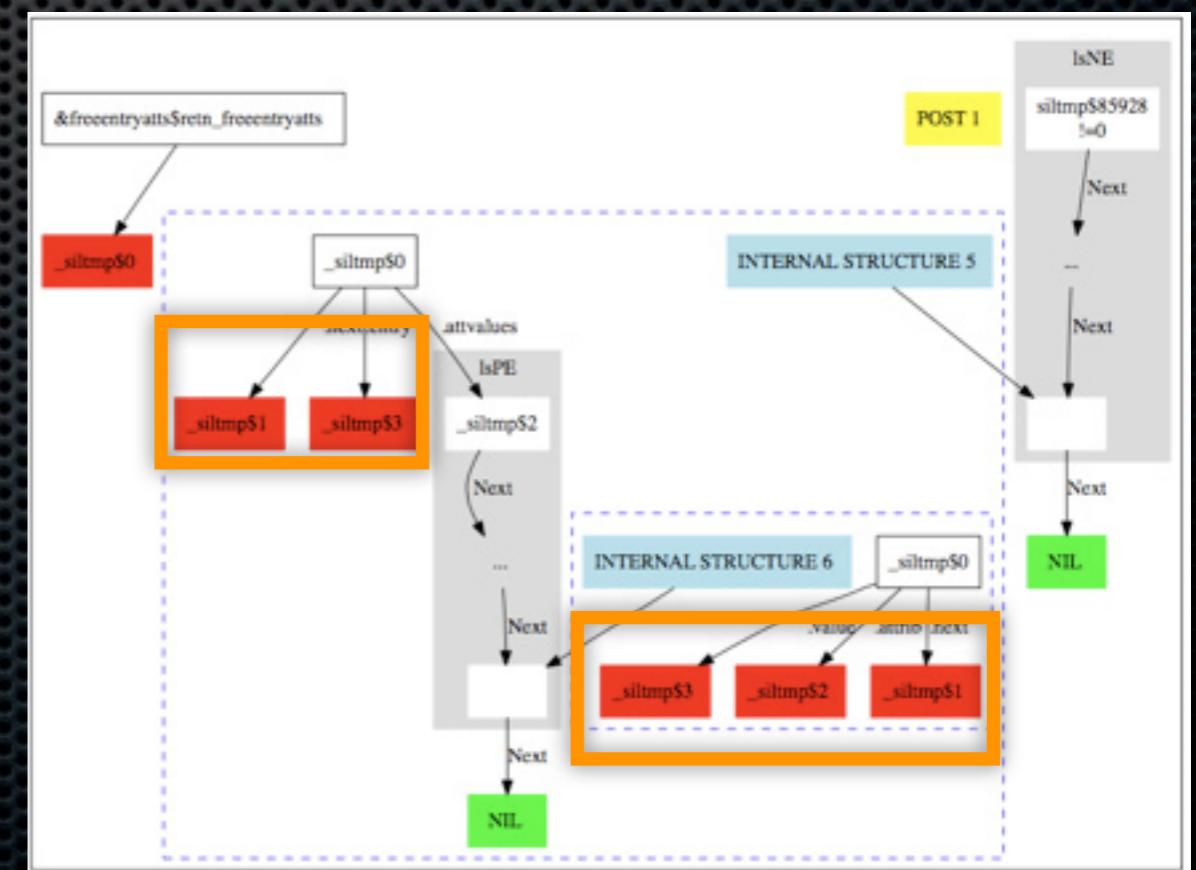
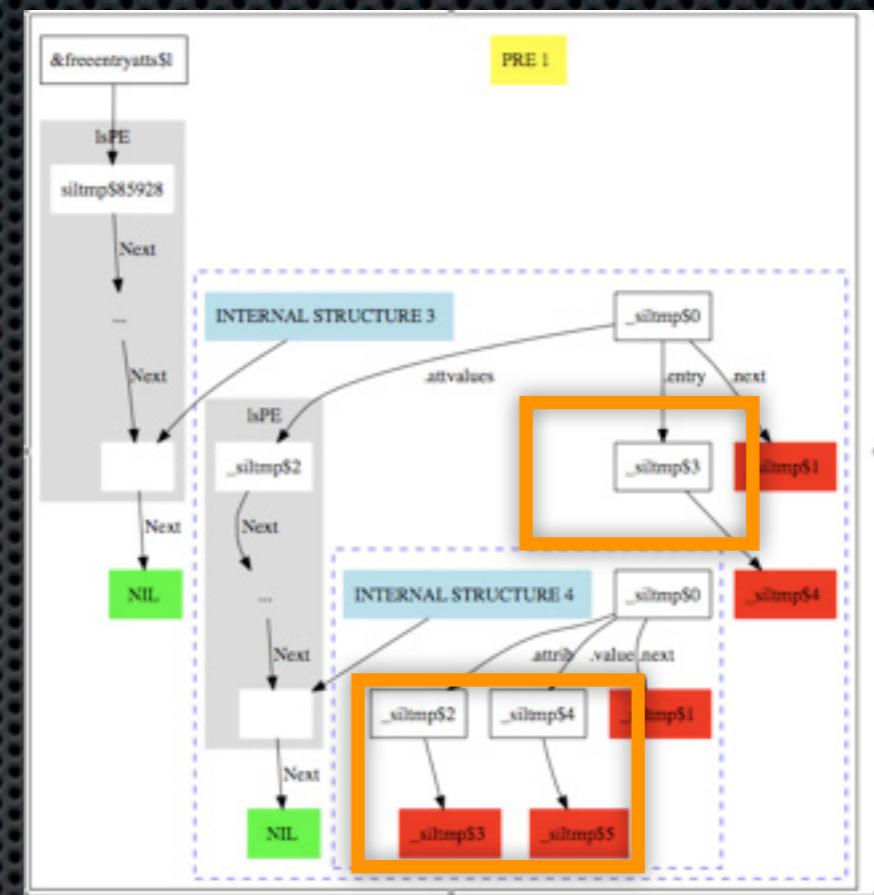
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The bi-abduction manifesto

- Frame inference $A \vdash B * X$ allows an analyzer to use small specs
- Abduction $A * X \vdash B$ helps to synthesize small specs
- Their combination, bi-abduction

$$A * X \vdash B * X'$$

helps to achieve compositional bottom-up analysis.
Furthermore it brings the benefits of local reasoning (as introduced in Separation Logic) to automatic program verification